



# Applied Mathematics For Experimental Science

**J.A. Sethian**

Head, Mathematics Department LBNL  
Simons Chair in Mathematics, Department of Mathematics, UC Berkeley

# Want to do two things:

**Provide an overview of CAMERA**

**Discuss detectors, data, mathematics, and models.**

# The Center for Applied Mathematics for Energy Research Applications (CAMERA)

**Mission:** Build the applied mathematics that can accelerate scientific discovery at DOE experimental facilities

**Execution:** Coordinated team of applied mathematicians, beam scientists, computational chemists, computer scientists, materials scientists, statisticians, image and signal processors, ...

**Initial set of partners:**



Advanced Light Source



Molecular Foundry



NCEM

**Initial Support: LBNL LDRD**

(P. Alivasatos, H. Simon, D. DePaolo, R. Falcone, D. Brown, J. Neaton, H.A. Padmore, M.J. Banda, K.A. Yelick)

**Now: Joint ASCR-BES Pilot Project**



(Steve Lee, P. Lee, B. Harrod, S. Binkley, H. Kung)



# Overview of CAMERA

## Build the advanced mathematics that can:

- Extract information from murky data, and help interpret experimental results
- Provide on-demand analysis as results are being generated
- Steer experiment and suggest optimal solutions
- Decrease turn-around time/save money: More experiments and more users
- Extend the capabilities of existing and future experimental facilities

## To do so, we need to:

- Have experimental scientists/applied mathematicians work together
- Develop common language
- Build new mathematical models, invent algorithms, build prototype codes
- Test on “shop floor”, iterate until codes are solid and useful

## Goal: Deliverables users can use (without becoming mathematicians):

Advanced mathematics embedded in useable software tools

# CAMERA: Organization

**ALS: Beam scientists**  
(D. Parkinson, A. Hexemer, S. Marchesini, D. Shapiro)

**Foundry/NCEM**  
(J. B. Neaton, W. Queen, D. Britt )

**LBL Math Department**  
(J.A. Sethian, C. Rycroft, J. Donatelli)

**LBLN Comp. Sci.**  
(S. Li, M. Haranczyk, H. Harikrishnan, T. Perciano, D. Ushizima, C. Yang)

**CAMERA**

**LBLN: Materials, Earth Sciences**

**LBLN/UCB: EFRC**  
(M. Haranczyk, J.B. Neaton, B. Smit)

**Berkeley Campus**

**EECS/Statistics Depts.**

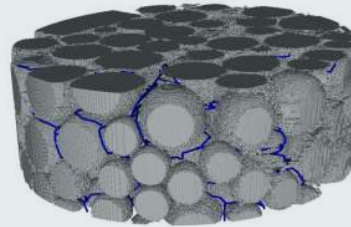
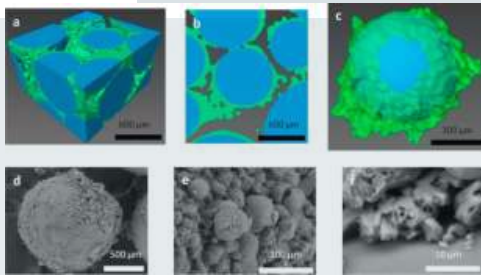
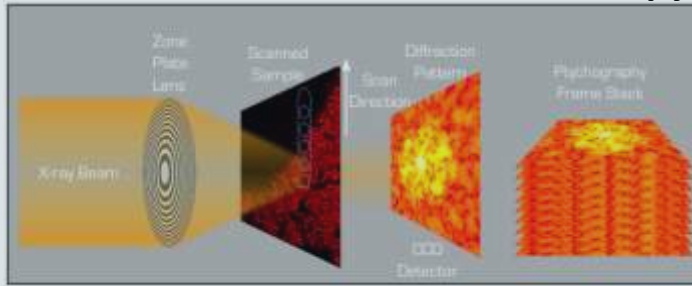
**Mathematics (Faculty/postdocs/grad students)**  
(J.A. Sethian, L. Lin, A. Grunbaum, E. van Andel, B. Preskill)

**BIDS (Berkeley Institute for Data Science)**

# CAMERA: Original/Current Projects

## Pytchography (ALS/MATH)

Coherent Diffraction with Microscopy

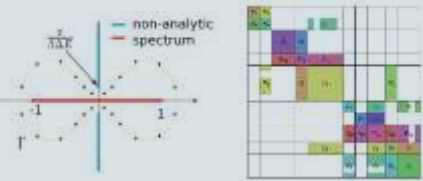


## Automatic Image Analysis (ALS/MATH)

## New methods for Density Functional Theory (MF/MATH)

$$H[\rho]\psi_i(x) = \left( -\frac{1}{2}\Delta + \int dx' \frac{m(x') + \rho(x')}{|x-x'|} + V_{xc}[\rho] \right) \psi_i(x) = \varepsilon_i \psi_i(x)$$

$$\rho(x) = 2 \sum_{i=1}^{N/2} |\psi_i(x)|^2, \quad \int dx \psi_i^*(x) \psi_j(x) = \delta_{ij}, \quad \varepsilon_1 \leq \varepsilon_2 \leq \dots$$



**GISAXS (ALS/MATH)** Grazing incidence small angle x-ray scattering

**Designer Materials (Molecular Foundry/Math)**

**X-Ray nanocrystallography (ALS/MATH)**

## **HipGISAXS:** ([http://camera.lbl.gov/software/hipgisaxs\\_software](http://camera.lbl.gov/software/hipgisaxs_software))

Flexible grazing-incidence small-angle X-ray scattering (GISAXS)  
Distorted wave Born approximation  
Speed: graphics processors and multicore processors.

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## **PEXSI** (<http://camera.lbl.gov/software/pexsi>)

Fast method for electronic structure calculation: Kohn-Sham DFT.  
Can regularly handle systems with 10,000 to 100,000 electrons.  
Achieves scalability on more than 10,000 processors..

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## **SHARP-CAMERA** ([http://camera.lbl.gov/software/sharp\\_camera\\_download](http://camera.lbl.gov/software/sharp_camera_download))

Multi-GPU Accelerated Ptychography Software .  
Combines diffraction + microscopy + high performance GPUS  
Advanced acceleration algorithms for convergence and analysis  
Freely available, open environment for collaboration/customization

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## **QUANT-CT** (<http://camera.lbl.gov/software/>)

Image enhancement, filtering, segmentation and feature extraction  
Currently on ALS beamline 8.3.2, multi GPU. Open source: Fiji plugin

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## **Zeo++** (<http://camera.lbl.gov/software/zeo/>)

Analysis/assembly of crystalline porous materials.  
Geometry-based analysis of structure/topology of material void space  
Current users: EFRC Nanoporous Materials Genome Center, EFRC  
Materials Project, Bosch, SABIC and Samsung.

# Outline of Talk

**How did this start?**

**History and Motivation**

**Why mathematics?**

**Math/Data/Computing**

**What is being delivered?**

**Four models for delivery**

**Where is it going?**

**A DOE Resource**



# Background: LBNL/UCB Mathematics:

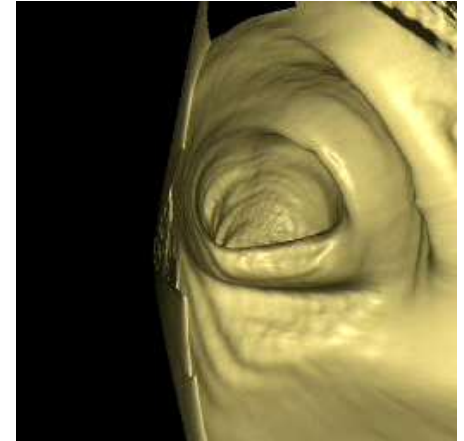
## Long Standing DOE Program: (LBNL+UC Berkeley)



Vertical Axis Wind Turbines



Cell Cluster Growth

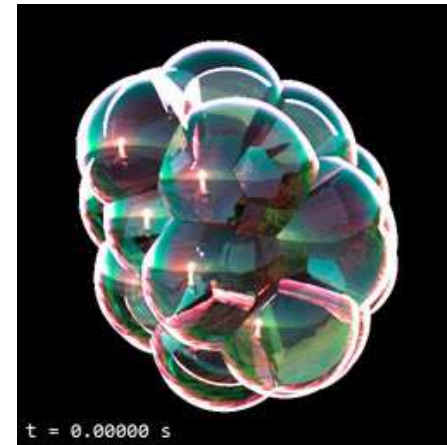
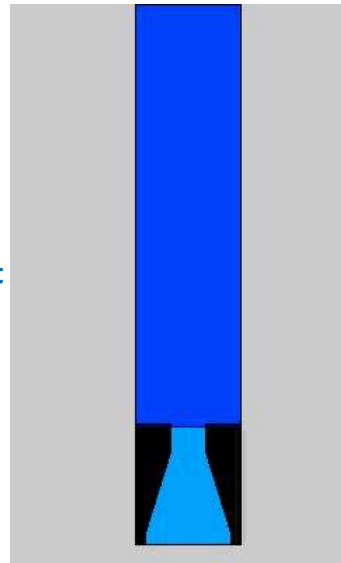


Virtual Colonoscopy



Draining in Coal Hoppers

Industrial Inkjet Printing



Industrial Foams

**Example: Semiconductor Algorithms: Samsung, Intel, Motorola, Infineon, Synopsis...**

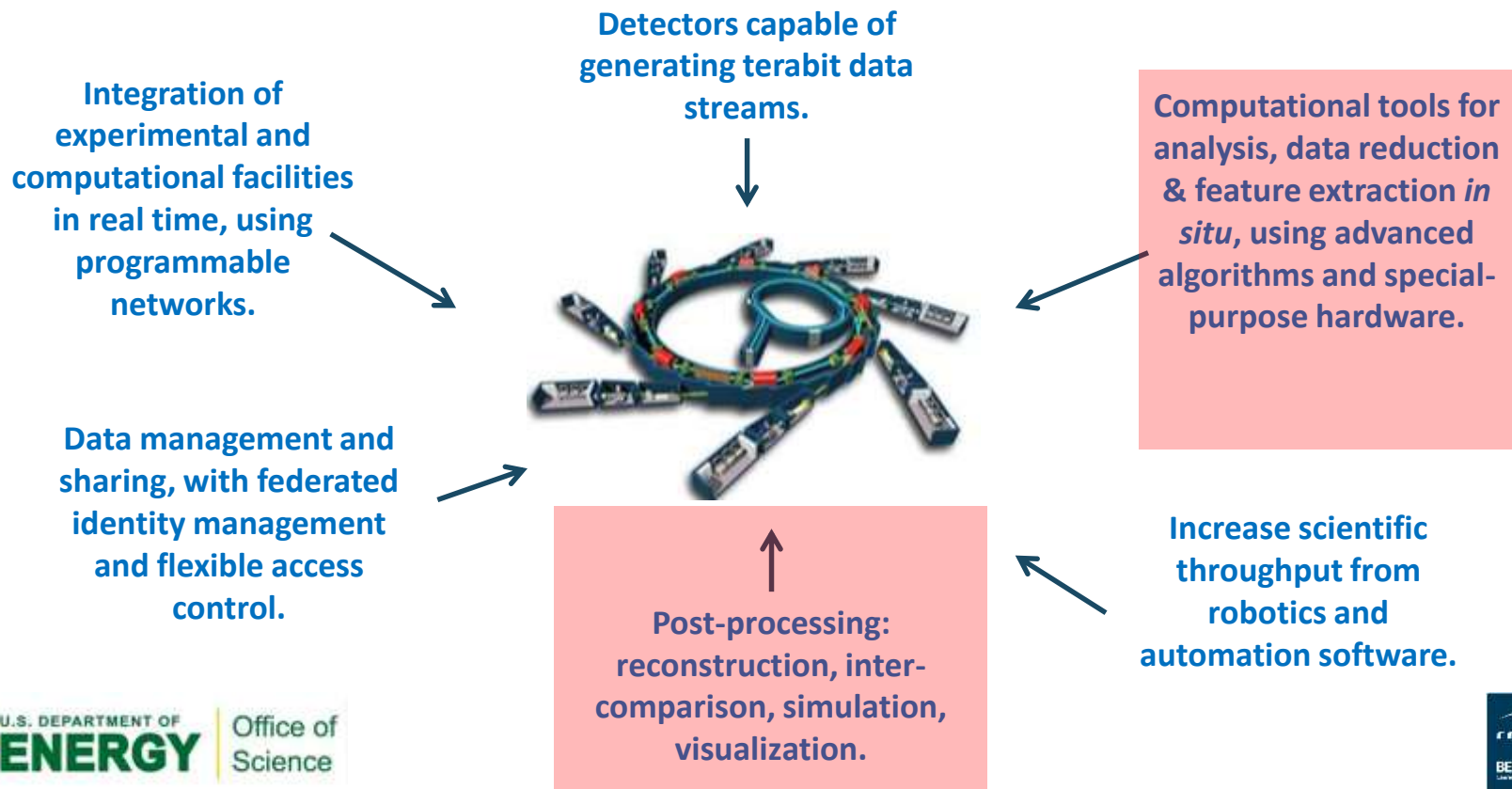
## A New Challenge from LBNL/Director

**Look broadly at mathematical needs of Office of Science facilities, starting with the ALS, Molecular Foundry, NCEM, Joint BioEnergy Institute (JBEI), and future facilities**

**Question: How can applied mathematics help facilities do  
More science  
More efficiently  
(users, materials, turn-around time...)?**

# DOE Facilities in 2025: More Data, More Users, More Discovery

Experimental facilities will be transformed by high-resolution detectors, advanced mathematical analysis techniques, robotics, software automation, and programmable networks.



# Mathematics for accelerating the analysis of experimental data

**Now**



**Later**

Computational tools for analysis, data reduction & feature extraction *in situ*, using advanced algorithms and special-purpose hardware.

Post-processing: reconstruction, inter-comparison, simulation, visualization.

## Mathematics for each can be quite different:

What is the minimum/fastest computational model/algorithm that gives (at least some) useful information?

Can you quickly determine if data is useful, not useful, or in between?

Can you quickly do analysis and steer experiment to more optimal configurations or output?

What is the maximal amount of information you can get out of the data?

Can data be measured, processed, organized and displayed to help understand/suggest further experiment?

Can data be transformed to initialize computational models, and output framed to complement experiment?

# Why is this so interesting (and challenging?)

- (a) Problems have not yet been “mathematicized”.
- (b) No “equations of motion”
- (c) Deep connections between the science and math

To tackle these problems requires new mathematics that bridges across mathematical disciplines.

Fortunately, Applied Mathematics is Undergoing a Profound Transformation

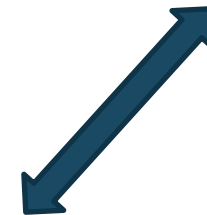
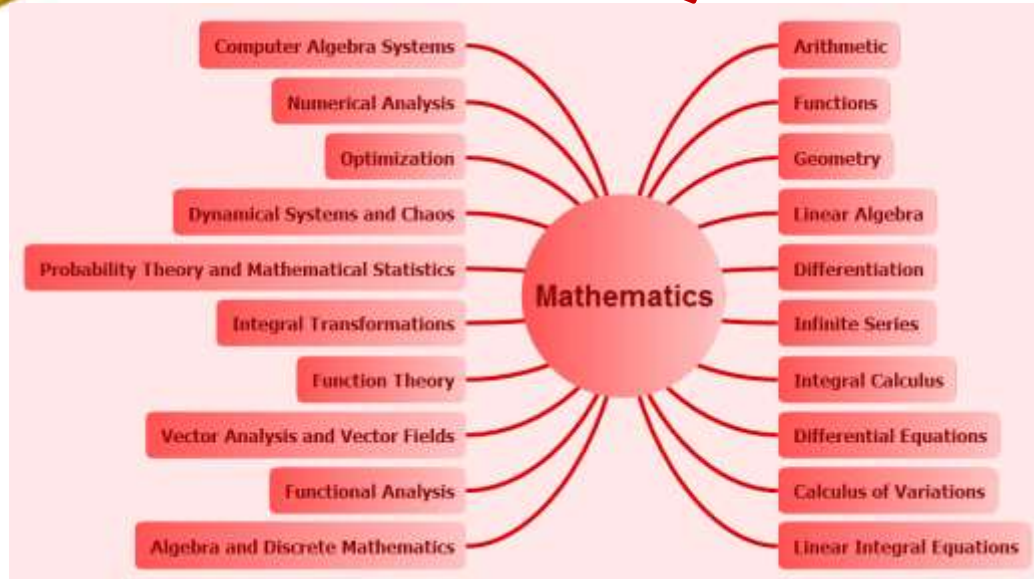
**Traditional walls** between continuous math, discrete math, analysis, probability and statistics, topology, algebra, geometry .... **are all breaking down.**

# Mathematics and (or versus!) “Big Data”

Data



Computers



Mathematics

Mathematics is what changes data into information

# Challenges are growing:

**More data, more resolution**

**More complexity**

**Less obvious relational linking**

**More noise**

**More false signals**

...

**Mathematics is what changes data into information**

**Going to need mathematics more  
than ever...**

**Today:**  
Facilities data is time-consuming

**Tomorrow:**  
More data. More quickly. High resolution.

**Critical need:**  
algorithms and analysis for *understanding*

**LBNL approach:**  
Focused teams of mathematicians/domain scientists

**New math to:**  
Guide and optimize experiments

Goal: Build the applied mathematics that helps *transform experimental data into understanding*

## Pilot Partners



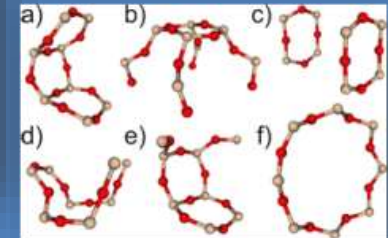
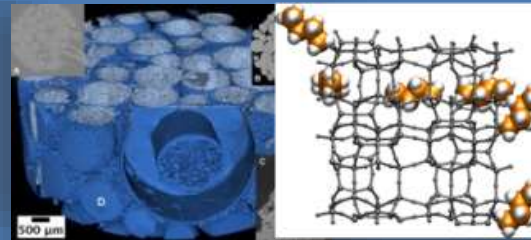
computing *structure* from imaging



analyzing samples and proposed new materials



designing new materials



**Key: Leverage state-of-the-art mathematics**

Spectral clustering	Maximum likelihood estimators	Graph theory	Machine learning	Mori-Zwanzig theory
Clique analysis	Computational harmonic analysis	Discrete Galerkin methods		
Hamilton-Jacobi solvers	PDE-based image segmentation	Statistical sampling	Discrete/continuous shape descriptors	
Voronoi methods	Representation theory	Bayesian analysis	Optimization methods	





# CAMERA: Personnel

## Who is working on this?

### Advanced Light Source (ALS):

- A. Hexemer (Beam Scientist/GISAXS)
- S. Marchesini (Ptychography)
- D. Parkinson (Beamline Scientist, Hard X-ray tomography)
- D. Shapiro (Beamline scientist)

### Molecular Foundry

- D. Britt (Organic and Macromolecular Synthesis)
- J. Neaton (Electronic Structure)
- W. Queen (Inorganic Nanostructures)

### National Center for Electron Microscopy (NCEM)

- P. Ercius (Scanning transmission electron microscope)

### Computational Research Division (CRD)

- M. Haranczyk (Materials Design)
- X. Li (GISAXS/)
- L. Lin (Electronic Structure)
- R. Martin (Materials Design)
- C. Yang (Electronic Structure)
- D. Ushizima (Image Analysis)
- T. Perciano (Image Analysis)
- H. Krishnan (Image Analysis/HPC)

### CRD Mathematics Department:

- J. Donatelli (X-Ray Nanocrystallography)
- C. Rycroft (Optimal Chemical Design)
- J.A. Sethian (Director)

**Opportunity: Steady stream of new Berkeley faculty/postdocs/grad students**

# What Does CAMERA Deliver?



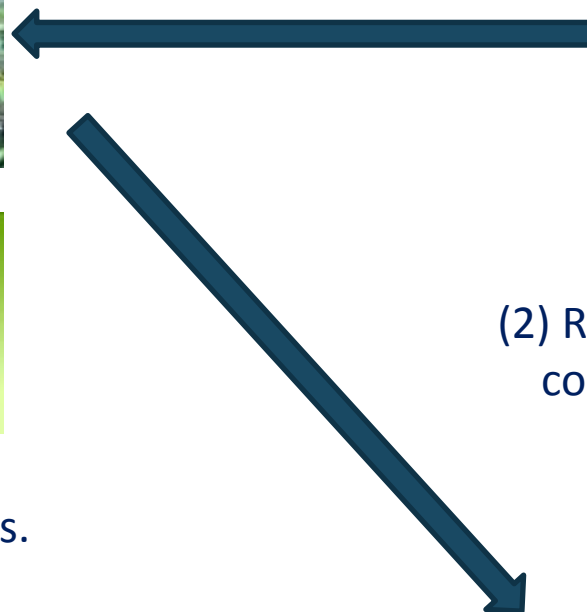
(1) Codes that run locally on computers embedded at facilities.



(4) Downloaded and run remotely.



(2) Remote browsers executing code locally running at facilities.



(3) Codes remotely run on data downloaded from facilities to supercomputer centers



# “Long-distance Delivery”: SPOT-Suite Led by C. Tull, LBNL

Towards an End-to-End Solution for Light Source Data, Analysis, & Simulation

- **Combining...**
  - scalable software systems.
  - HPC/HTC/network resources.
  - advanced algorithms & analysis.
  - advanced simulation.
  - realtime feedback.
- **Multi-division team: CRD, ALS, Math, CAMERA, ESN, MSD, & NERSC.**
- **Extending to include SAXS,  $\mu$ Diff, and Ptychography beamlines.**  
Focus on in-situ, time-resolved experiments, new algorithms, data sharing & collaboration.
- **SC14 Demos include LCLS, APS, NSLS datasets.**

**Research into generalizable real time workflows and metadata already yielding valuable insight for photon scientists.**





# Who is using CAMERA's deliverables?

## **Ptychography:**

CXRO/SEMETEC, LLNL/NASA, UI Chicago, UC San Diego, UC Davis, UCB, McMaster, Stanford. ALS, BNL, F. Maia, Uppsala, BYU, multiple workshops, tutorials

## **QuantCT:**

Advanced Light Source Users, available on “shop floor”.  
Downloadable Fiji Plugin (world-wide user base).

## **PEXSI:**

Accelerated Kohn-Sham Density Functional Algorithms  
Embedded in SIESTA (**Spanish Initiative for Electronic Simulations with Thousands of Atoms**): **Next: CP2K**

## **Zeo++:**

Open-source package - [www.zeoplusplus.org](http://www.zeoplusplus.org). Zeo++ : a default tool for two BES Materials Genome Centers (Nanoporous Materials Genome Center (Minnesota) and Center for Functional Electronic Materials (LBNL)) and LBNL EFRC for Gas Separations Roughly 200 registered users world-wide in both academia/industry (e.g. Bosch, Samsung)

## **HipGISAXS:**

ORNL, ANL, ALS, Molecular Foundry, numerous universities, ...





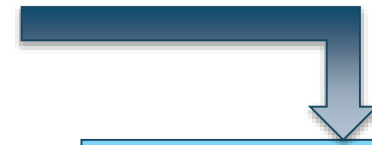
# AN OVERVIEW OF SOME OF THE WORK UNDERWAY

Application



Mathematical  
issues

New mathematics  
we needed to  
build and exploit



Software  
for Users

(Describe problem, emphasize new mathematics,  
describe deliverables)

# SHARP

(Scalable Heterogeneous Adaptive Robust Ptychography)

## Fast scalable methods for ptychographic reconstructions

S. Marchesini, D. Shapiro (Advanced Light Source)

H. Krishnan (LBNL Computing Sciences)

F. Maia (LBL/Uppsala)

H-T Wu (LBNL/Stanford, now Toronto)

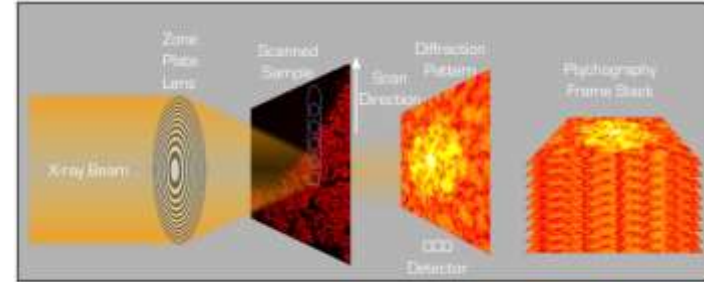


S. Marchesini, D. Shapiro, H. H. Krishnan (LBL) F. Maia (LBL/Uppsala), H-T. Wu (Stanford))

## Combine Coherent Diffraction with Microscopy

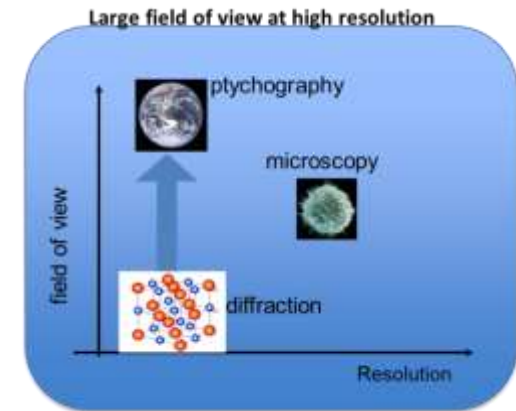
### Fundamental idea: combine:

- High precision scanning microscope with
- High resolution diffraction measurements.
- Replace single detector with 2D CCD array.
- Measure intensity distribution at many scattering angles



### Each recorded diffraction pattern:

- contains short-spatial Fourier frequency information
- only intensity is measured: need phase for reconstruction.
- phase retrieval comes from recording multiple diffraction patterns from same region of object.



### Ptychography:

- uses a small step size relative to illumination geometry to scan sample.
- diffraction measurements from neighboring regions related through this geometry
- Thus, phase-less information is replaced with a redundant set of measurements.

**Lots of ptychographic equipment/codes throughout DOE, universities, world-wide**

### When does it (not) work?

(no convergence proof yet available for method)

### Existing algorithms may have trouble converging on large data sets:

(iterative methods intrinsically operate by interchanging information between nearest neighbor frames (diffraction patterns) at each step, so it might take many iterations for frames far apart to communicate.)

### Effects of noise and physical uncertainties:

(how do reconstruction algorithms perform with uncertainties in photon statistics, lens perturbations, illumination positions, incoherent measurements, detector response and discretization, time fluctuations, etc.)

### What is the best lens and illumination scheme for arbitrary specimens?

(given a detector, with a limited rate, dynamic range and response function, what is the best scheme to encode and extract more information per detector channel?)

**Tackling Efficiency: Challenges with basic alternating projection algorithm:**

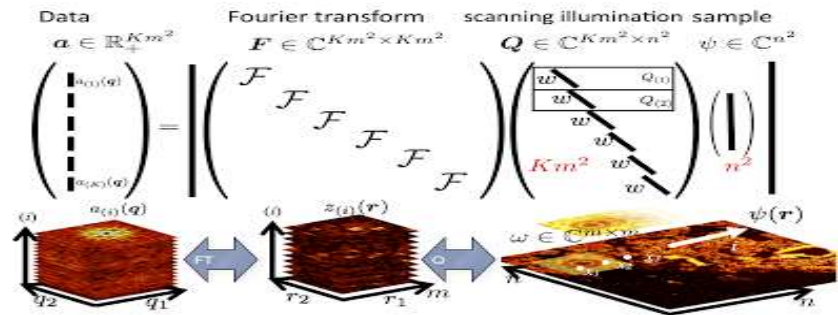
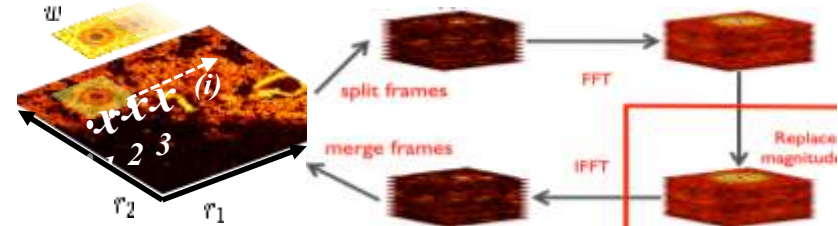
**Poor scaling:**

long range interactions among frames decay exponentially with distance.

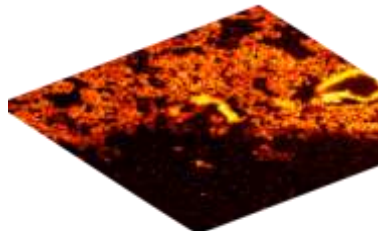
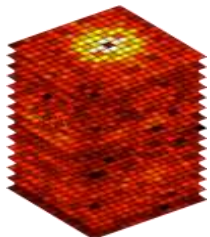
**Poor initial guess:**

can significantly delay convergence.

**Ultimately, an overdetermined problem in high dimensional space.**



Short-time Fourier Transform



Large dimensional data

Low dimensional space

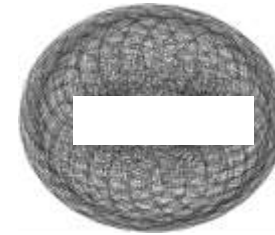
**How can we speed this up?**



## Building a better starting guess:

(1) View every pixel of every frame as a dimension.  
Each data point lives on a torus (complex plane)

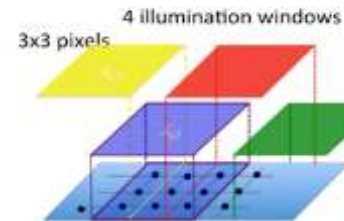
Diffraction data manifold



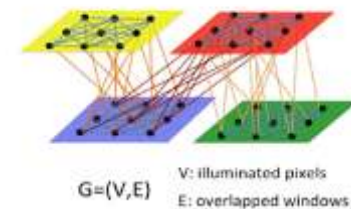
Approximate torus with ball

(2) Build “relationship network RN: a graph (V,E) that relates each frame to its neighbors.

measurement model



measurement graph



(3) Construct Graph Laplacian of RN: defined as difference between the degree matrix  $D$  and the adjacency matrix  $A$ :  $GL = D - A$

(4) The largest eigenvector of the Connection graph provides the most aligned phases encoding the (approximate) data topology.

**This provides a strong starting guess.**

# Released Code: SHARP: Scalable Ptychography Solver

## Code: Open source, downloadable package

release    prototype    under way/testing

- Scalable code, ( source package,  remote interface,  web interface,  API).
- real time feedback by reducing latency
- 80x speedup with algorithms
- 30x speedup with GPUs
- >16x speedup with distributed GPU
- Optimal Network fabric design for throughput
- Optimal lens design for SNR
- Iterative tomography ( network/bandwidth optimized)
- Chemical mapping (robust PCA/SVD)
- Dynamics

**Software presentations:** Ptycho 2013, FIO/LS, SIAM IM14, MSPPR, XRM, Coherence 14

**Software tutorials:** Coming: SSRL/CAMERA xx/2014, CAMERA/ALS/BNL AUG 2014

CAMERA/ALS/APS Sep 10/14, COHERENCE, XRM, SIAMIM, FIO/LS,

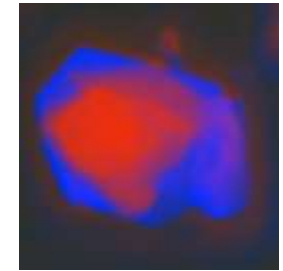
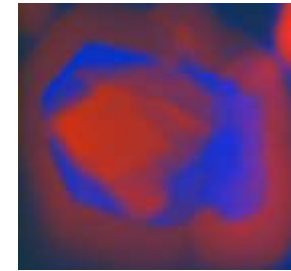
RACIR summer school, ALS Users workshop

## “Compute design”

SHARP real time specs:

- 3D torus p2p fabric
- CCD/RDMA streaming
- instrument calibration

**Intercalation Battery Research:  
Mechanisms in Lithium Ion Phosphate  
ALS BL 5.3.2 (Nat. Phot. /in press)**

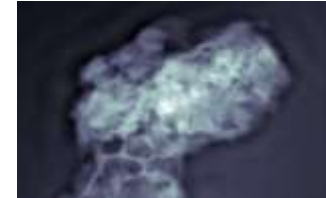


## Partners:

CXRO/SEMETEC, LLNL/NASA, UI Chicago, UC San Diego, UC Davis, UCB, McMaster, Stanford. ALS, BNL, F. Maia, Uppsala, BYU

## Currently

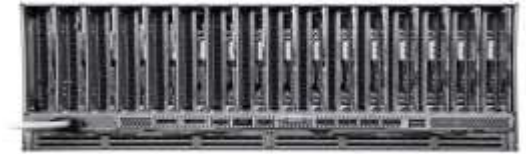
the user interface starts processing at the end of a full scan. (1 minute each)



Processing: 60x60 (1024<sup>2</sup>) frames/minute

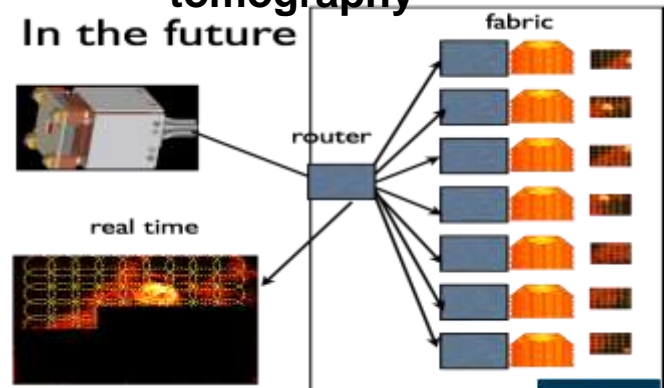
## In the future

**low Latency** (<5 ms) feedback by streaming detector frames on distributed direct memory access fabric.



**High bandwidth 3D torus p2p**  
For hyperspectral ptycho tomography

Real time enables smart self-calibrating, auto-tuning feedback of the microscope control system.



**Two Weeks Ago: Finished a prototype “Real Time” version-code directly off of CCD**

# QuantCT

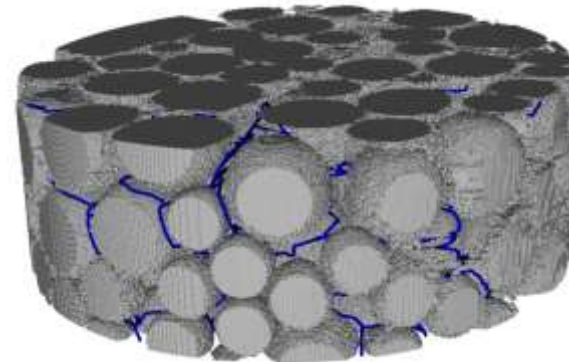
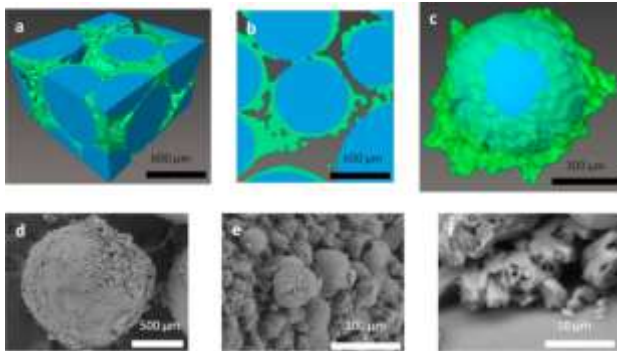
## Automatic image analysis tools for micro-CT

D. Ushizima, D. Morozov, H. Krishnan, T. Perciano (LBNL Computing Sciences)  
D. Parkinson (Advanced Light Source)

**Goal: Develop algorithms for 3D/4D quantitative analysis of experiments, addressing challenges posed by noise, artifacts, sheer size, and heterogeneous materials.**

**Analyze structure: porosity, pathways, interior voids, ...**

- Application: High-resolution synchrotron-based X-ray absorption microtomography.
- Suitability of materials and biomineralization processes for carbon sequestration.
- Acquire projection views at equi-spaced angles: produce 2D cross-sections.
- Gray level value of image voxels reflects x-ray attenuation and density.
- Compute pathways through materials:



Imaging Pipeline Requires:

- Filtering: remove noise, sharpen contrasts (**bi-lateral and non-linear filters**)
- Segmentation to isolate, and extract shapes from images (**PDE-VIIM methods**)
- Feature detection/analysis (**Reeb graphs, topological analysis, channel detection**)



2011

2014

Filtering of microCT

Segmentation of (near) homogeneous regions

Analysis of microstructures

Get rid of  
artifacts

Get structure  
from clutter

Get  
parameters  
from grains

- (1) **Mumford-Shah functional** for image segmentation of two phases  
(index  $i$  indicates separate phases, Find interface  $\mathbf{G}$  to minimize  $E$ )

$$E(\mathbf{G}, I_1, I_2) = \int_A (I(x, y) - I_1)^2 d\mathbf{x} + \int_B (I(x, y) - I_2)^2 d\mathbf{x} + m \int_G g(\mathbf{G}(s)) ds$$

- (2) **Becomes PDE transport method using level set methodology:**

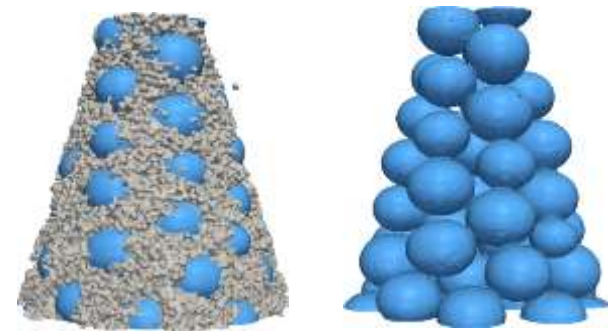
$$f_t + F |\nabla f| = 0, \text{ where } F = [((I - I_1)^2 + ((I - I_2)^2) - m \nabla \cdot (g \nabla f / |\nabla f|)]$$

- (3) **New approach: Extend the Mumford-Shah energy**  
functional to multi-phase multi-interface

### Voronoi Implicit Interface Method (VIIM)

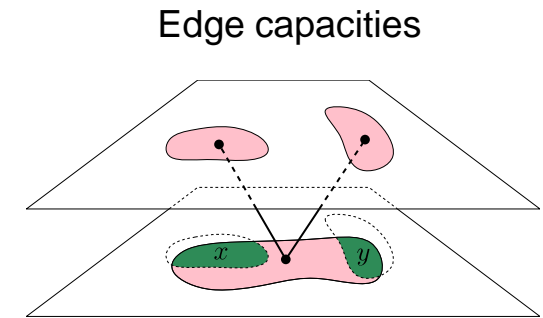
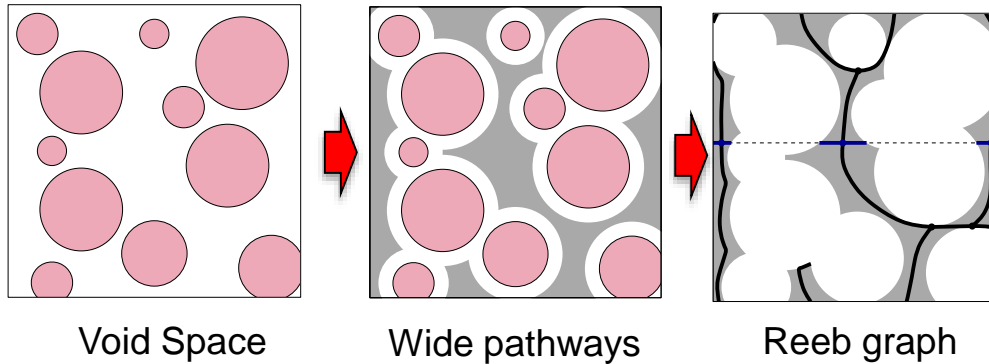
$$F_i = [((I - I_i)^2 - m \nabla \cdot (g \nabla f / |\nabla f|)]$$

(combination implicit embedding plus dual Eikonal Voronoi reconstruction)



- (4) **Allows simultaneous extraction**  
**of multiple structures in 3D.**

## Augmented Topological Descriptors: Max Flow Graphs and Persistence Diagrams

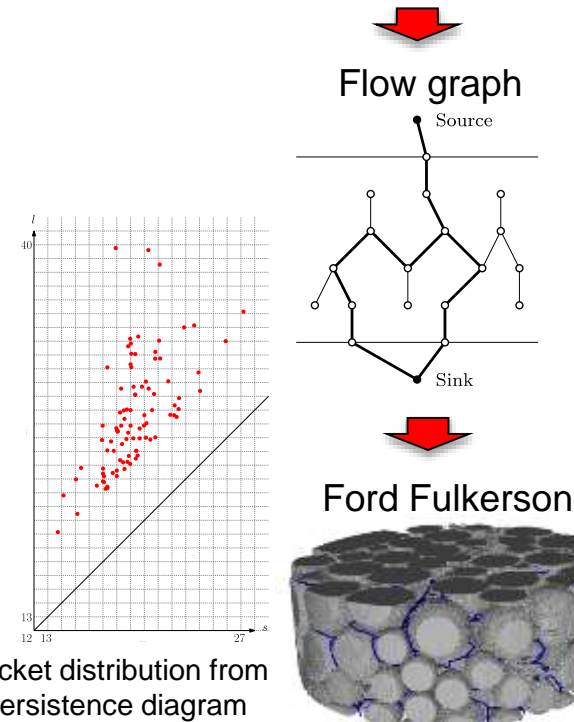


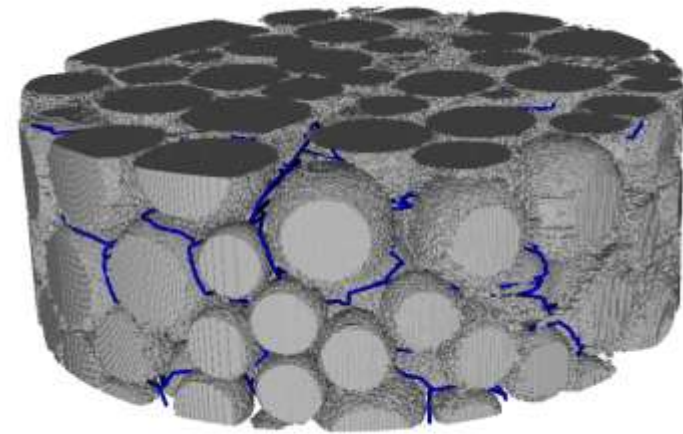
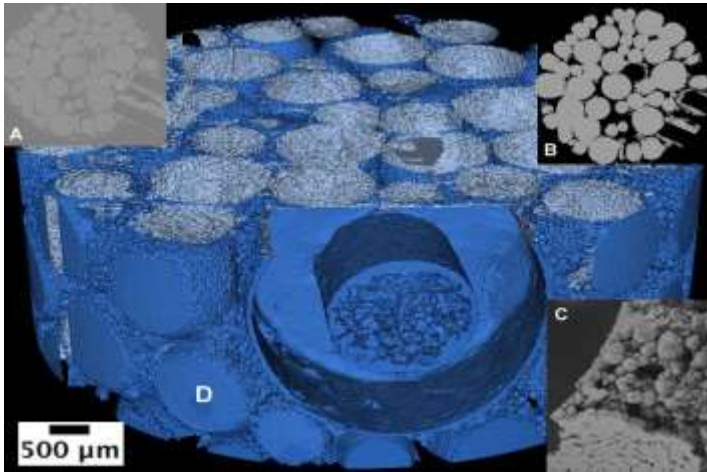
### Max-Flow:

- Reeb graph: Evolution of level sets of function on manifold.
- Use to detect pathways for particle of size  $a$
- Edge capacities = Intersection area between slices
- Flow between source/sink without exceeding capacities
- Family of graphs: Vary  $\alpha$

### Persistence Diagram:

- Track components in superlevel set of distance function
- When component merge: “younger” component merges into “older” component

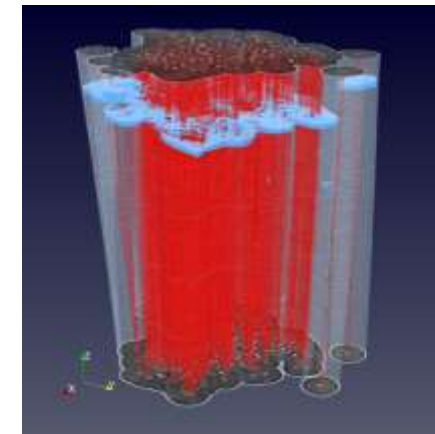
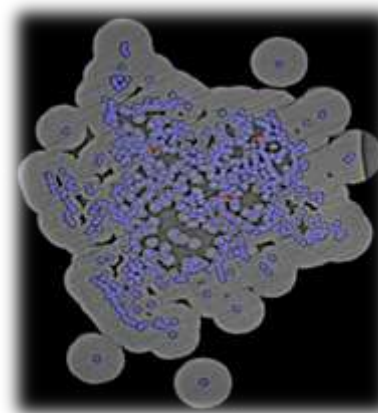
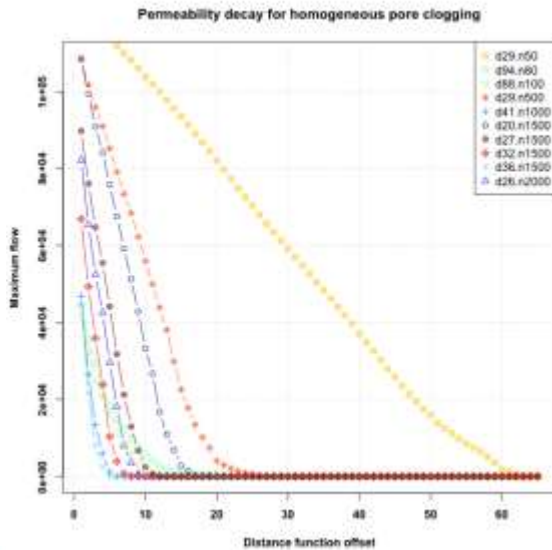




Pore network through porous material

QuantCT

software for microCT analysis (0.33 images/s)



Automatic detection of 3D fibers and matrix cracking from assembled 2D slices

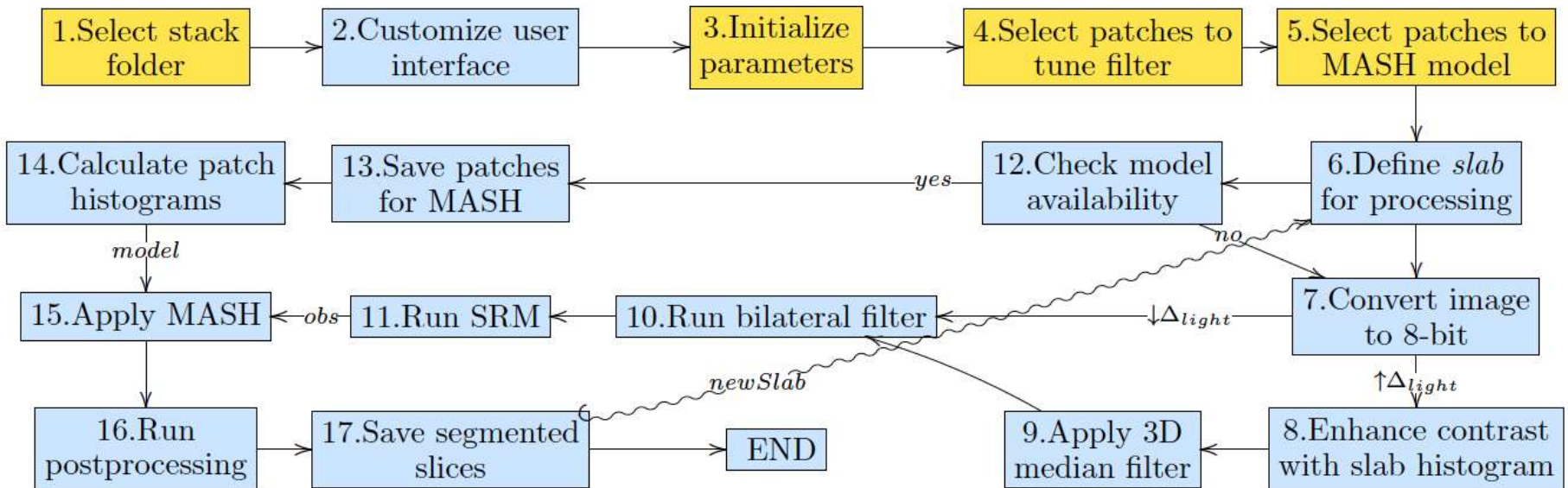


Figure 1: Flow diagram of Quant-CT segmentation workflow: yellow indicates user-interaction event and blue indicates a program action.

**Ref.** Ushizima, D.M., Bianchi, A.G.C, deBianchi, C., Bethel, W., "Material science image analysis using quant-CT in ImageJ", in: ImageJ User and Developer Conference, 2012.



# QuantCT: Delivery Mechanisms



## Delivery mechanisms:

Current:

- (1) Browser/computer at ALS
- (2) Available as Fiji plugin
- (3) Prototype source downloadable.

## Code Specifics:

- Implemented in Java.
- Part of *Fiji* framework.
- Implemented in *OpenCL*.
- Called from Java code through *JOCL*.
- Dedicated thread assigned to each OpenCL device to handle multiple accelerators on any given node.
- Each thread requests unprocessed slices up to the maximum allowed by the hardware.

QuantCT – splitting volumes into VOID and DENSE MATERIAL

Enter parameters to process, segment and analyze microCT images:

Stack folder:

Output folder:

Filename radix:

Images: parameters to subset stack with 484 images

First slice at:  max=484

Testing subset:  max=484 <= SUBSET SUGGESTED

Training subset:  max=50

Slab size:  images

Algorithm: parameters to filter and segment stack

Sigma range:  [0,255]

Sigma spatial:  -1 for interactive tuning

Minimum area:  pixels

Complexity of SRM:  [2,64]

Boolean classification? \* Multiclass under construction

Keep previous settings? \*\* Use file settings.txt in the specified folder

Subset stack with cylinder? \*\*\* Consider only portion inside the cylinder

Considerable brightness variation across slices? \*\*\*\* Normalization applies

QuantCT

Cancel OK

Ref. **Ushizima**, Parkinson, Nico, Ajo-Franklin, Macdowell, Kocar, Bethel and Sethian, *Statistical segmentation and porosity quantification of 3D X-ray microtomography. Applications of Digital Signal processing XXXIV, Vol. 8135, pp.1-14 (2011).*

# Fluctuation X-Ray Scattering

## Mathematics for structure reconstruction

J. Donatelli, J.A. Sethian (LBNL Computing Sciences)

P. Zwart (LBNL Advanced Light Source and Physical Biosciences)



# Fluctuation X-Ray Scattering

## (Brand-new work)

- (1) Fluctuation X-Ray Scattering:
  - Extension of Small- and Wide- angle X-Ray Scattering
  - X-Ray snapshots taken below rotational diffusion times
  - Significantly more experimental information than traditional techniques
  - Powerful technique for modern synchrotrons and free electron lasers (FEL)
- (2) Going from real space structure to fluctuation scattering data is straightforward.
- (3) But the reverse “inverse” problem is tough.
- (4) A joint CAMERA collaboration between LBNL Physical Biosciences, ALS, and Computing Sciences has produced a new technique: “**M-TIP**”, which exploits multi-tiered iterative phasing and solves this inverse problem.
- (5) The new method figures out structure of objects that cannot be crystallized, at a far higher resolution than previously available (to appear: PNAS in few weeks)
- (6) Example: Using **M-TIP**, was able to reconstruct 3D profile of pentameric ligand-gated ion channel (pLGIC), from Protein Data Bank entry 4NPP





# CAMERA: Where is this going?

## Reaching out:

### Positive response from the community

BESAC Committee Presentation (June 2014)

Oak Ridge/SNS Joint NSRC Workshop (June 2015)

“Big, Deep, Smart Data Analytics in Materials Imaging”

Brookhaven and NSLS (May 2015)

Invited Seminar Talk

Argonne/APS Joint Workshop (March 2015)

“Frontiers in Data, Modeling, and Simulation

LBNL/Advanced Light Source (Oct. 2014)

“CAMERA Workshop on Real-Time Robust Ptychography”

### Many software requests:

Download, use CAMERA codes

Requests for CAMERA to house, curate, and host algorithms and software across the light sources

### New Joint Projects starting up:

GISAXS and extensions to neutron sources (ORNL/SNS)

Ptychography (BNL, ANL)

Fluctuation scattering (LCLS)

Knowing what to build, how to build it, and how to use it requires close-knit, coordinated teams with many different skills.



With careful attention to mathematics and algorithms, we can build codes and software tools that can transform data into the information that users really want.

[camera.lbl.gov](http://camera.lbl.gov)

