



**Northern Illinois
University**

Electron Cooling for an Electron Ion Collider: Computational Methods and Code Development

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DOE-NP Accelerator R&D PI Meeting

October 20, 2017

Main Goals



- Proof of principle **demonstration of electron cooling** with the **first particle-level detailed** simulations (Jones Report:: line 3: High, A)
- **Develop a high-performance code** with these capabilities, and other beam dynamics challenges beyond cooling (Jones Report:: line 4: High, A)
- **Applications** to electron-ion collider (MEIC/LEIC) modeling, design, and optimization (Jones Report:: line 39: High)

Expenditures and Milestones



| | FY10+FY11 | FY12+FY13 | FY14+FY15 | FY16+FY17 | TOTALS |
|-----------------------------|-----------|-----------|-----------|-----------|--------|
| Funds Allocated | 0+56 | 55+52=107 | 50+54=104 | 50+50=100 | \$367K |
| Actual Costs to Date | 56 | 107 | 104 | 100 | \$367K |

| | FY17 | FY18 |
|------------------|--|--|
| Quarter 1 | Shared memory parallelization of FMM data structures and integration with parallel FMM | Electron cooling simulations in the JLEIC pre-booster at injection |
| Quarter 2 | Variable order Picard integrator with automatic step size control parallelization | Electron cooling simulations in the pre-booster at extraction energy |
| Quarter 3 | Binned time step implementation in parallel | Setup the re-circulator ring optics and bunched cooling in COSY |
| Quarter 4 | Parallel PHAD integration, benchmarking and optimizations | Study electron beam dynamics in the re-circulator ring, set maximum useful turn limits |

Cooling as an N-Body Problem



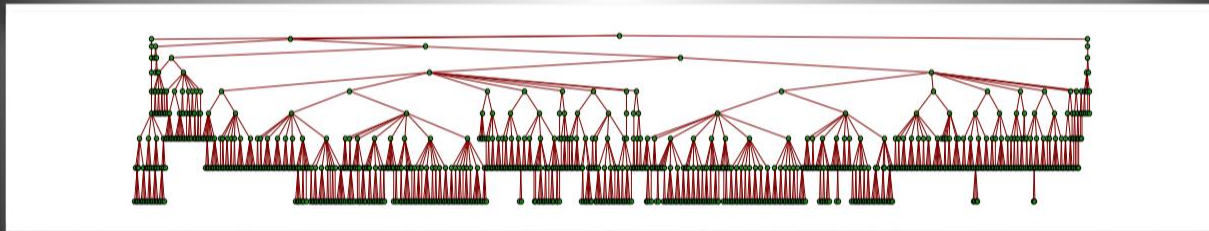
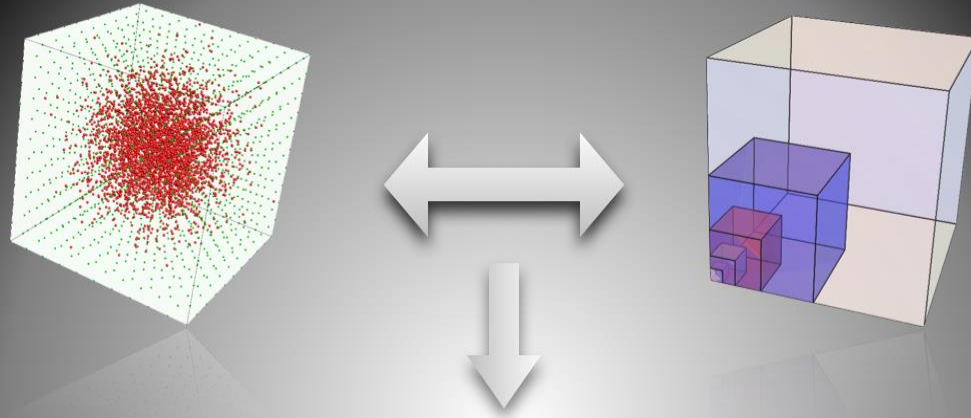
- Many **collective beam dynamics** effects can be cast in the form of an N-body problem: space charge, intra-beam scattering, electron cloud, beam-beam, beam-plasma, etc.
- **Electron cooling** is one of the most challenging:
 - Accurate analytical estimates are difficult to come by
 - Large particle numbers, but far from statistical limits
 - Both attractive and repelling forces
 - Close encounters are rare but matter



Main Challenges of an N-Body Solver

- **Efficient Force Computation**
 - ✓ Adaptive hierarchical space decomposition
- **Accurate Time Stepper**
 - ✓ Variable high order, adaptive integrators with automatic steps size and order selection, and dense output
- **Ability to deal with very large N**
 - ✓ Distributed, high performance computing on hybrid architecture supercomputers
- **Ability to deal with long time-scale dynamics**
 - ✗ Time does not parallelize

The Fast Multipole Method



“Best” Algorithms

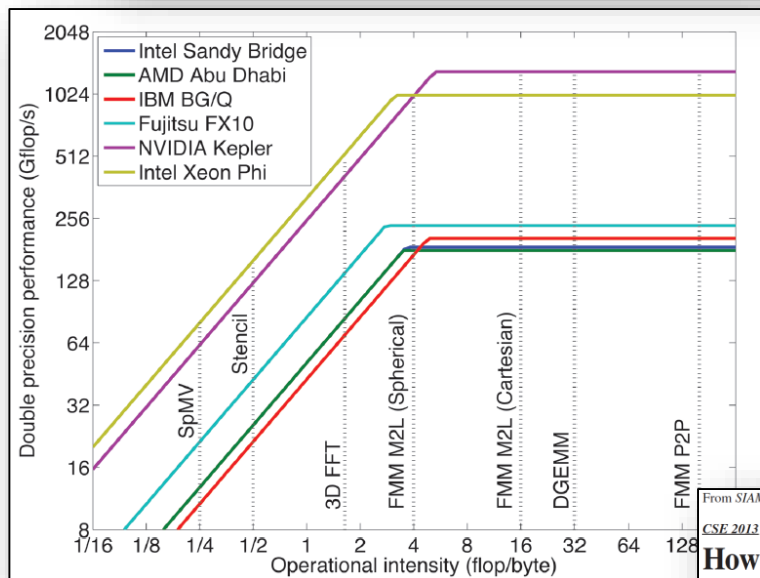


Comparison of scalable fast methods for long-range interactions

Phys. Rev. E **88**, 063308 – Published 19 December 2013

Axel Arnold, Florian Fahrenberger, Christian Holm, Olaf Lenz, Matthias Bolten, Holger Dachsel, Rene Halver, Ivo Kabadshow, Franz Gähler, Frederik Heber, Julian Iseringhausen, Michael Hofmann, Michael Pippig, Daniel Potts, and Godehard Sutmann

Our findings suggest that, depending on system size and desired accuracy, the FMM- and FFT-based methods are most efficient in performance and stability.

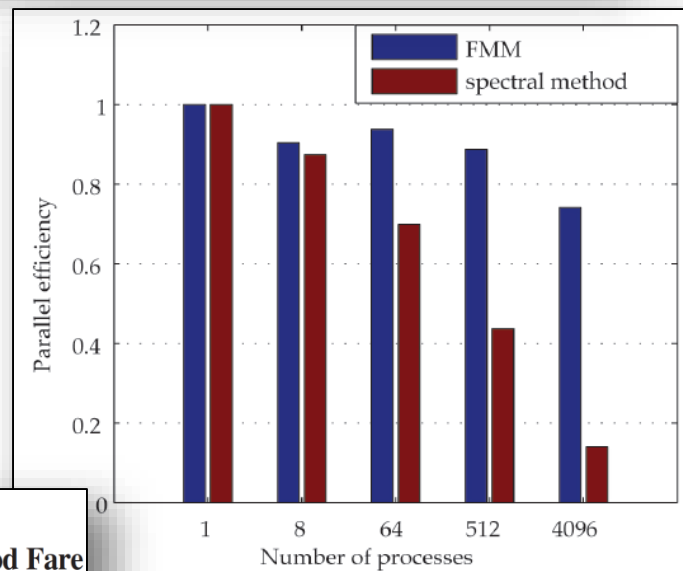


From *SIAM News*, Volume 46, Number 6, July/August 2013

CSE 2013

How Will the Fast Multipole Method Fare in the Exascale Era?

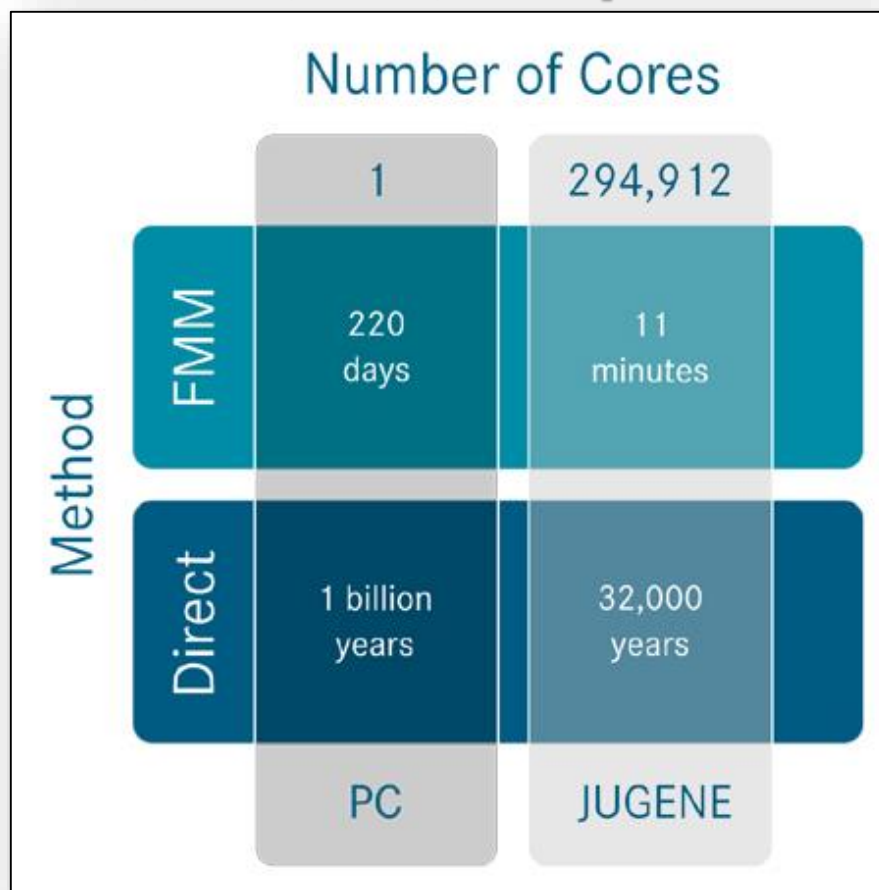
By Lorena A. Barba and Rio Yokota



FMM World Record



3,011,561,968,121 particles



Credit: Jülich Supercomputing Centre (JSC)

Picard Integrator



- Picard iterations are used to prove existence and uniqueness of solutions of ODEs
- We implemented it in a Differential Algebraic framework to make it efficient numerically, and variable order to adjust for user requested accuracy
- Not adaptive, hence cannot handle well close encounters and more than one particle species

$$y' = ty^2, y(0) = 1.$$

$$y(t) = y(0) + \int_{t_0}^t sy(s)^2 ds$$

$$Y_0(t) = 1.$$

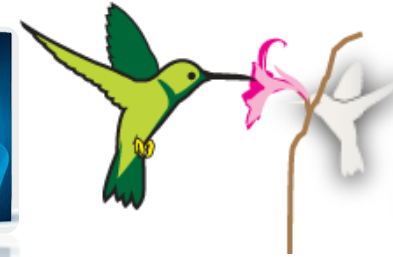
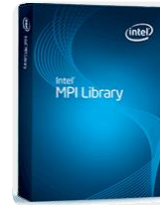
$$Y_1(t) = 1 + \int_{t_0}^t s(-1)^2 ds = 1 + \frac{1}{2}t^2.$$

$$Y_2(t) = 1 + \int_{t_0}^t s(-1 + \frac{1}{2}t^2)^2 ds = 1 + \frac{1}{2}t^2 - \frac{1}{4}t^3 + \frac{1}{24}t^6.$$

$$\begin{aligned} Y_3(t) &= 1 + \int_{t_0}^t s(1 + \frac{1}{2}t^2 - \frac{1}{4}t^3 + \frac{1}{24}t^6)^2 ds \\ &= 1 + \frac{1}{2}t^2 - \frac{1}{4}t^4 + \frac{1}{8}t^6 - \frac{1}{24}t^8 + \frac{1}{96}t^{10} - \frac{1}{576}t^{12} + \frac{1}{8064}t^{14} \end{aligned}$$

Particles' High-order Adaptive Dynamics (PHAD)

We developed, and continue to improve, a parallel code (PHAD) based on these new methods that will be the first one capable of particle-based simulations of electron cooling and other difficult beam dynamics phenomena with high fidelity, efficiently.



NORTHERN ILLINOIS UNIVERSITY

Center for Research Computing & Data

Division of Research and Innovation Partnerships



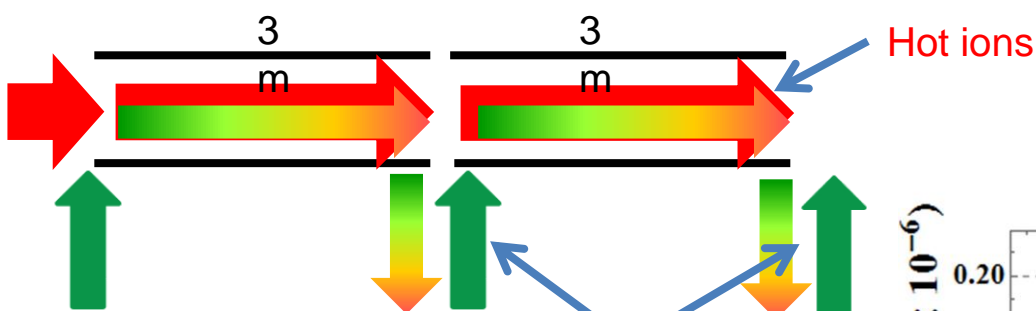
NORTHERN ILLINOIS UNIVERSITY

Beam Physics Code Repository

N. Illinois Center for Accelerator & Detector Development

<http://niu.edu/beamphysicscode/>

Electron Cooling Simulations



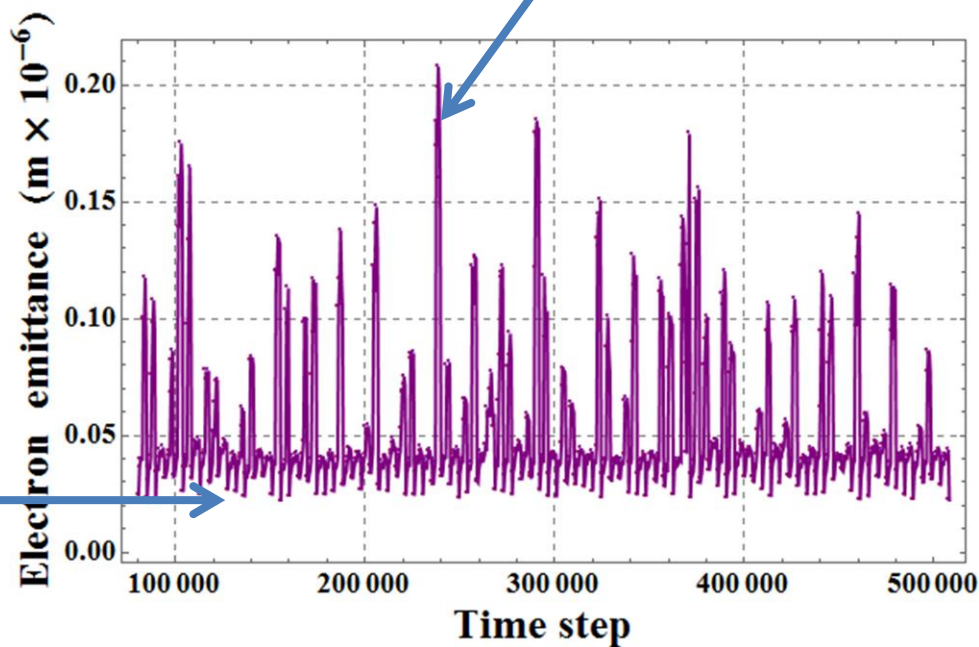
3m equivalent to
~4700 time steps

Fresh cold
electrons

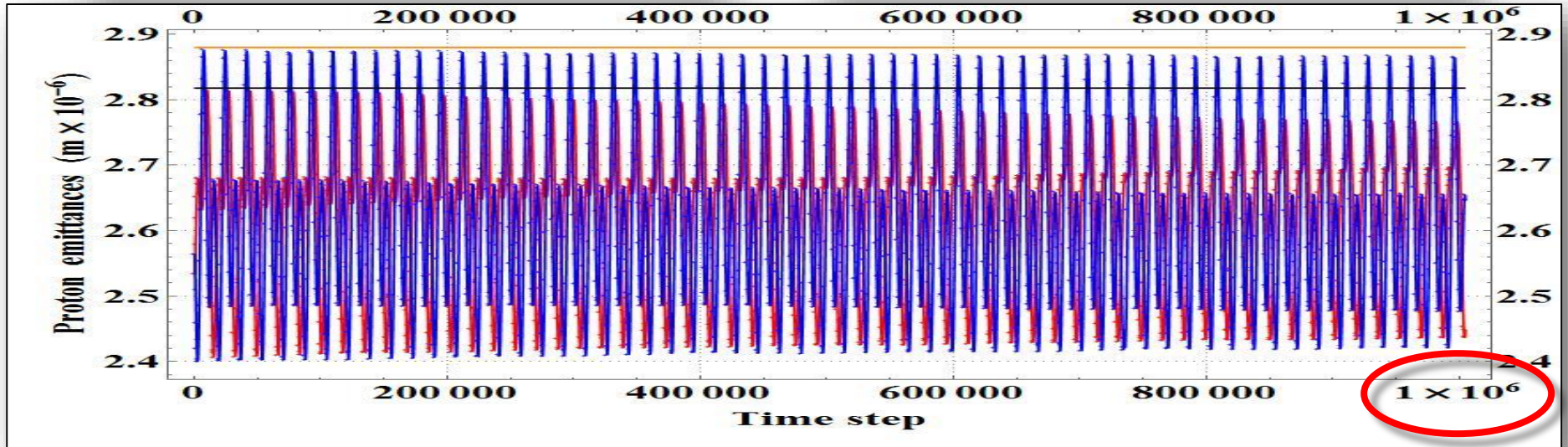
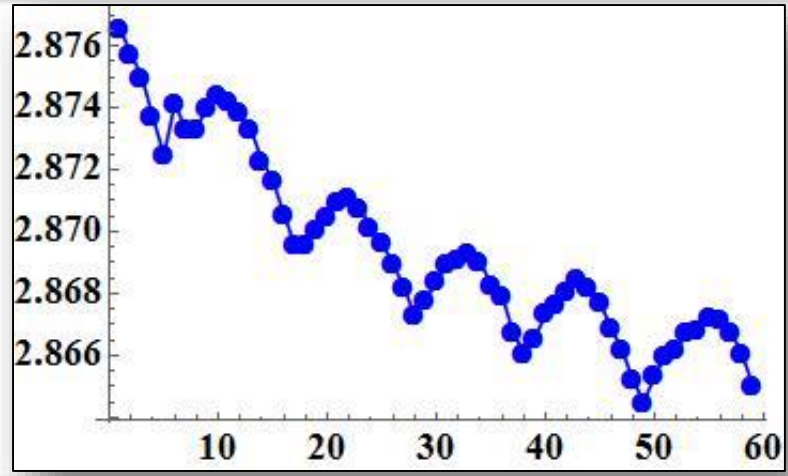
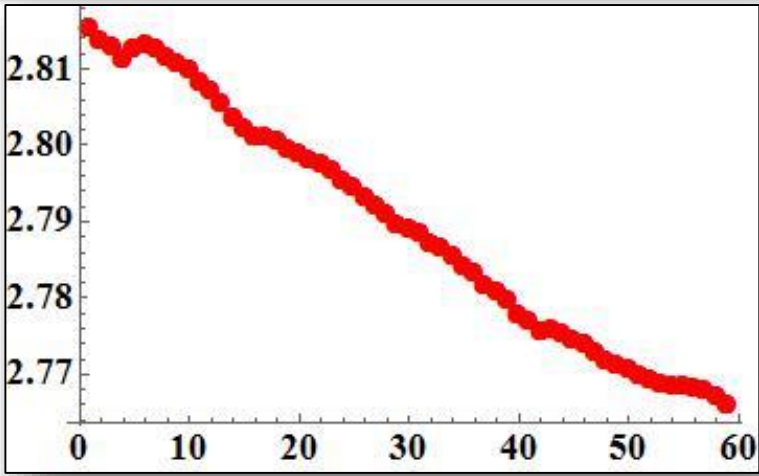
Fresh electron
bunches have low
emittance

Hot ions

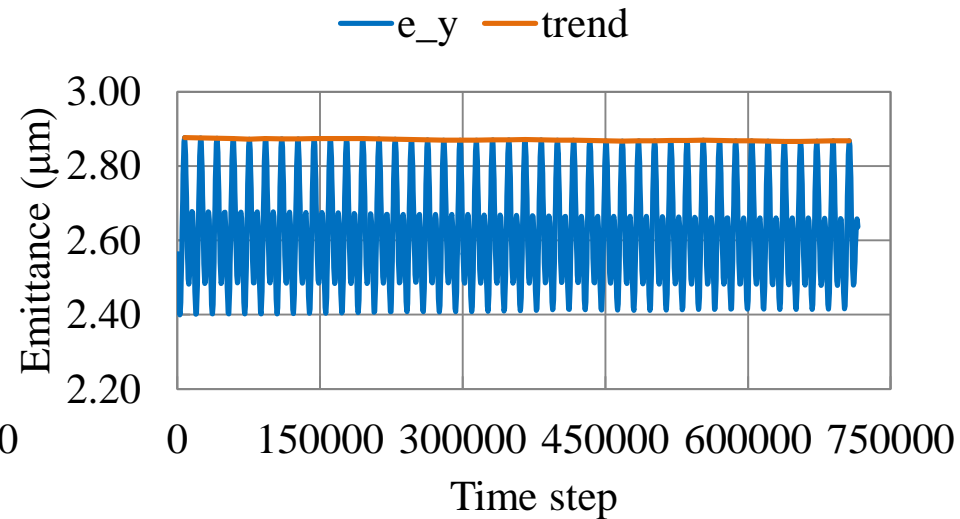
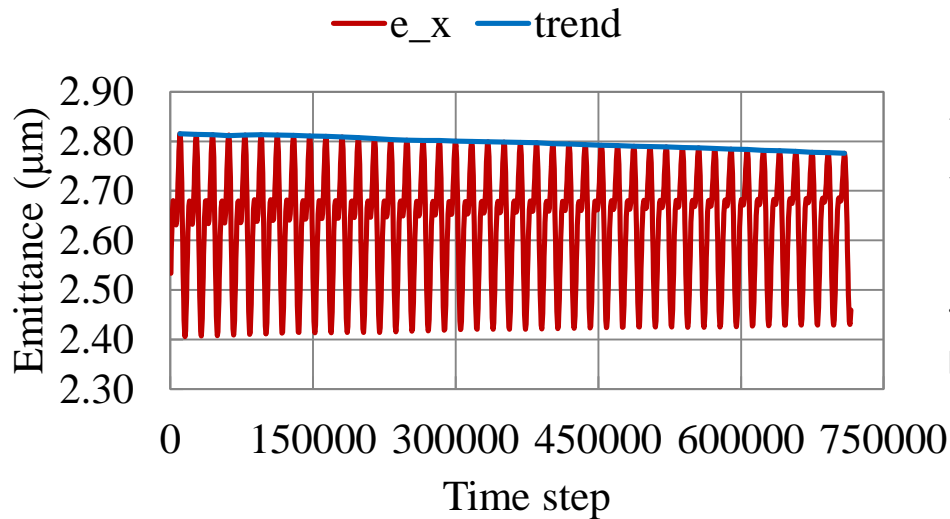
Spent electron bunches
have large emittance



First Particle-Level Cooling Simulation



Cooling with Solenoidal Field

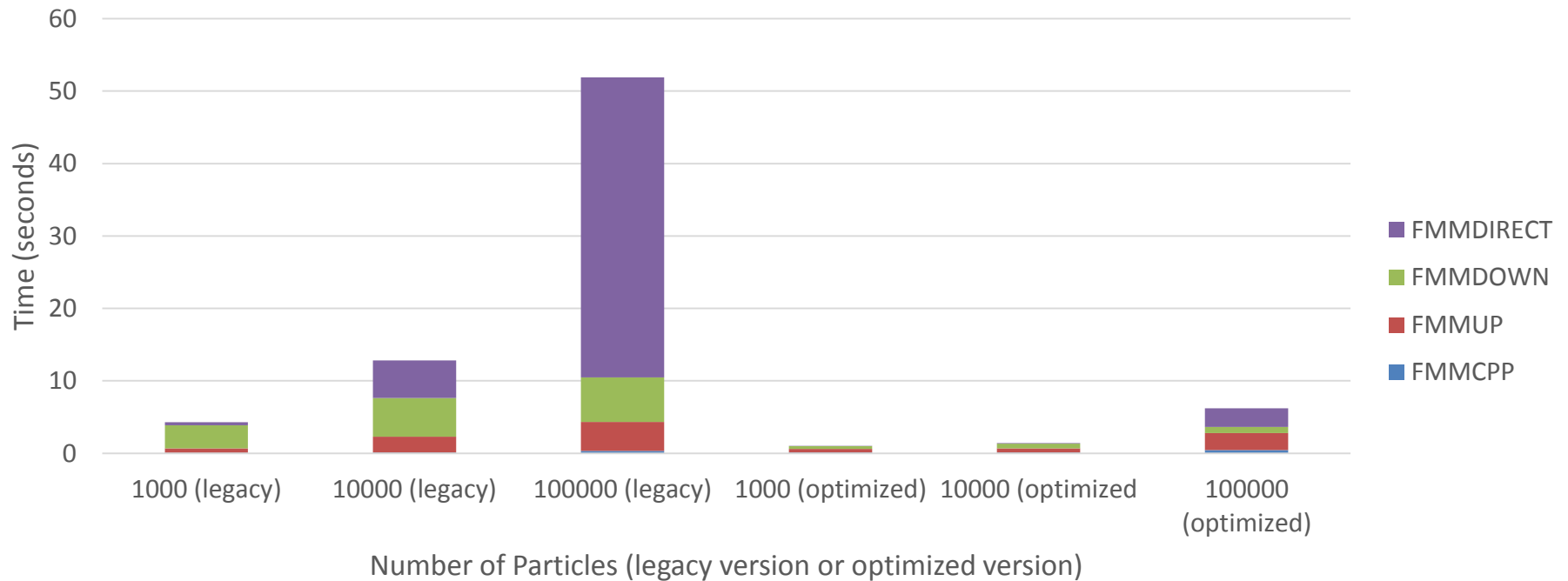


X emittance and Y emittance decrease faster with time

FMM Parallel Efficiency Improvements



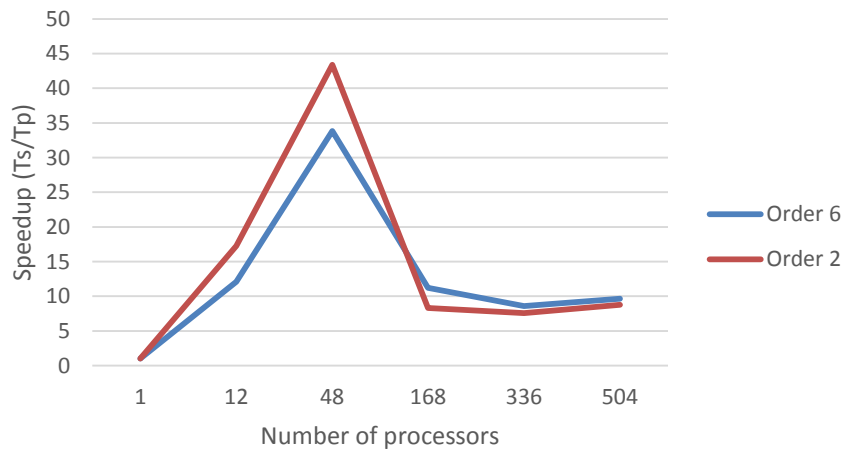
Runtime vs Number of Particles



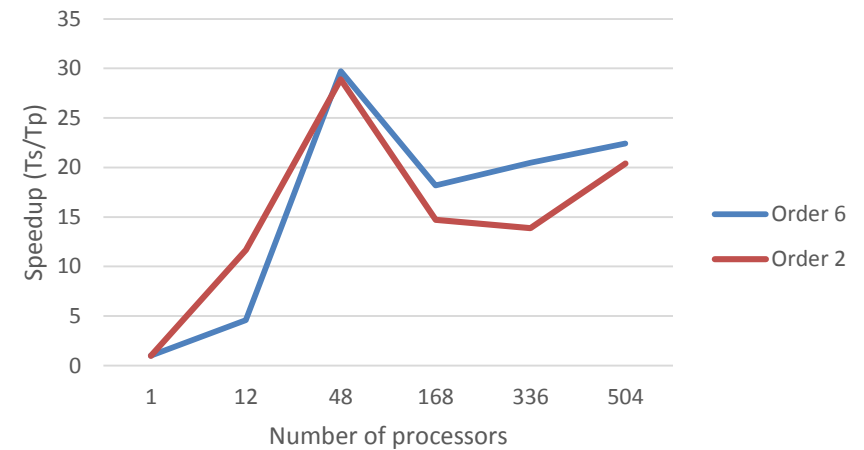
Parallel FMM Speedup (preliminary)



100,000 Particles Speedup FMM_MPI avg



1,000,000 Particles Speedup FMM_MPI avg



Adaptive, Variable Order Integration

Proposition . Assume that the function $h \mapsto x(t_m + h)$ is analytic on a disk of radius ρ_m , and that there exists a positive constant M_m such that

$$|x_m^{[j]}| \approx \frac{M_m}{\rho_m^j}, \quad \forall j \in \mathbb{N}.$$

Then, if the required accuracy ε tends to 0, the optimal value of h that minimizes the number of operations tends to

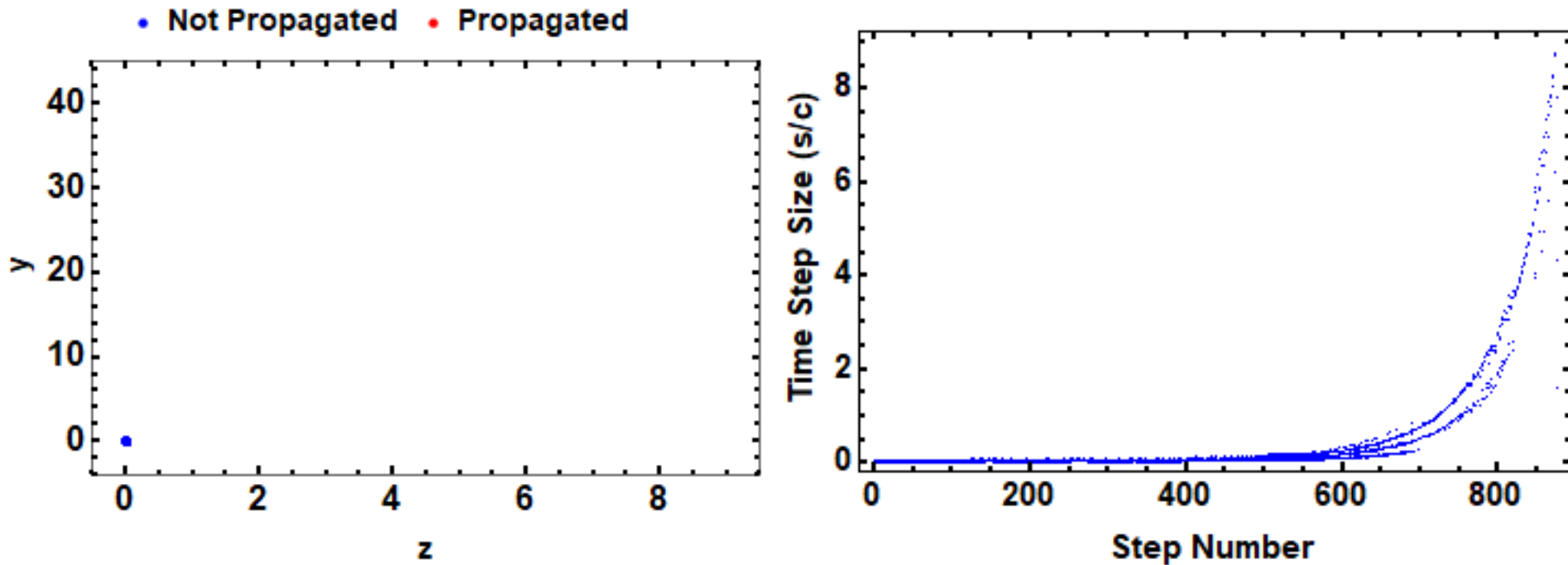
$$h_m = \frac{\rho_m}{e^2},$$

and the optimal order p_m behaves like

$$p_m = -\frac{1}{2} \ln \left(\frac{\varepsilon}{M_m} \right) - 1.$$

Simo (2001)

Low Energy Protons in Electric Field



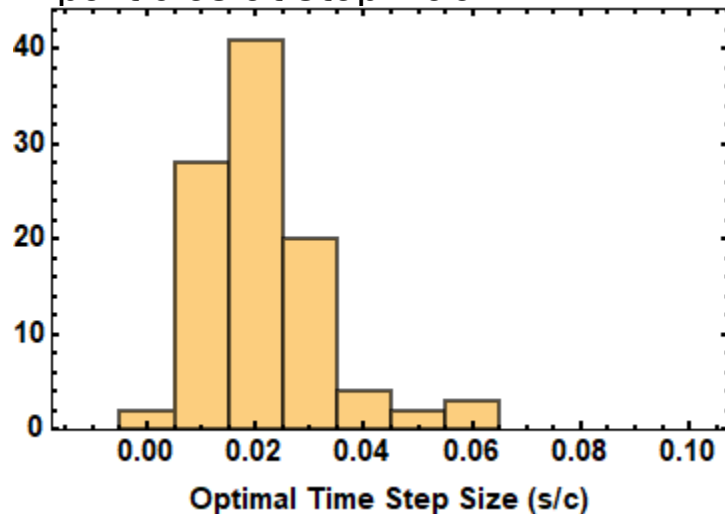
Accuracy setting $\varepsilon = 10^{-12}$

Optimal Time Step Sizes

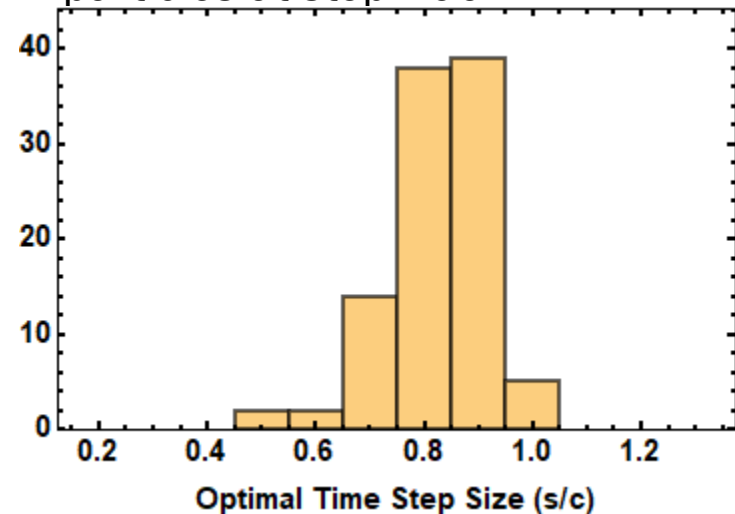


- Optimal Step sizes at later steps are larger than at earlier steps because the particles move away from each other

- Optimal time step sizes for all particles at step 100



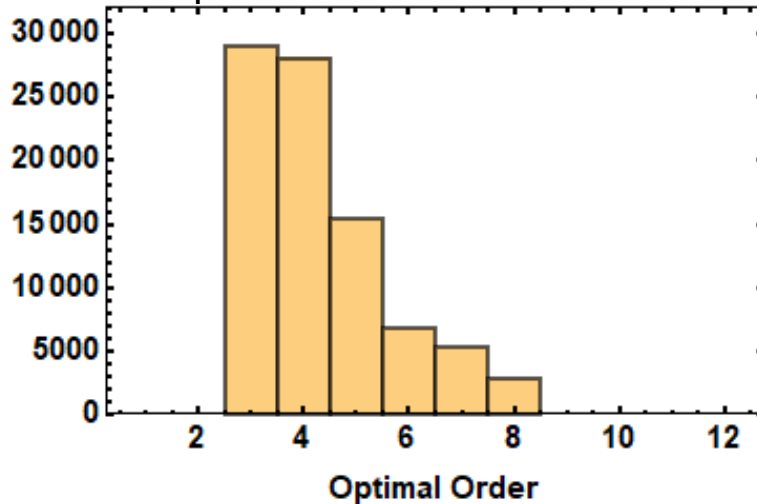
- Optimal time step sizes for all particles at step 700



Optimal Orders

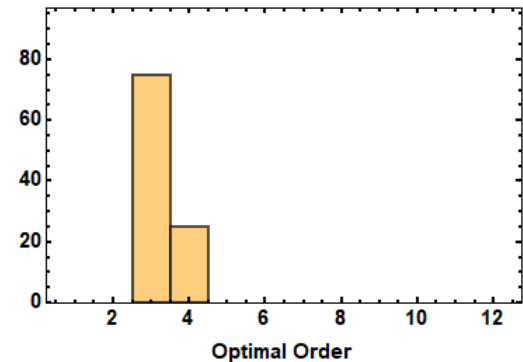


- Optimal orders of all particles at all steps

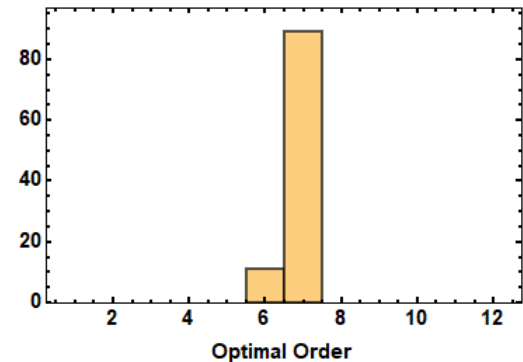


- Orders are varied to achieve the given accuracy efficiently

- Optimal orders of all particles at an early step



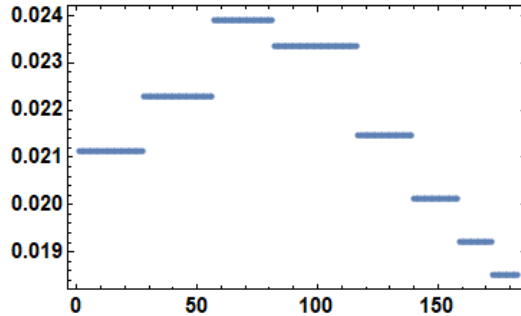
- Optimal orders of all particles at a later step



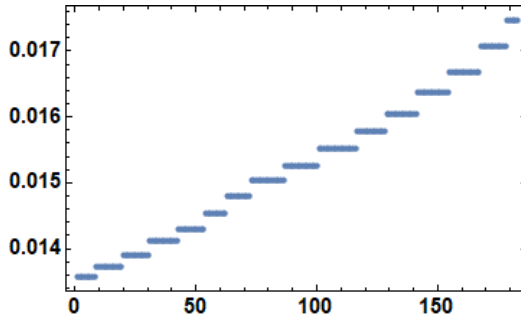
Optimal Time Steps of Some Protons in a High Energy Bunch



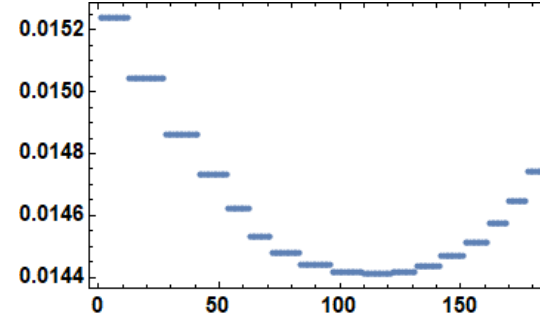
- Particle # 5000



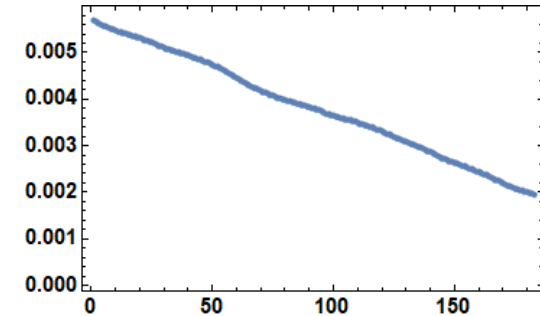
- Particle # 3000



- Particle # 9000



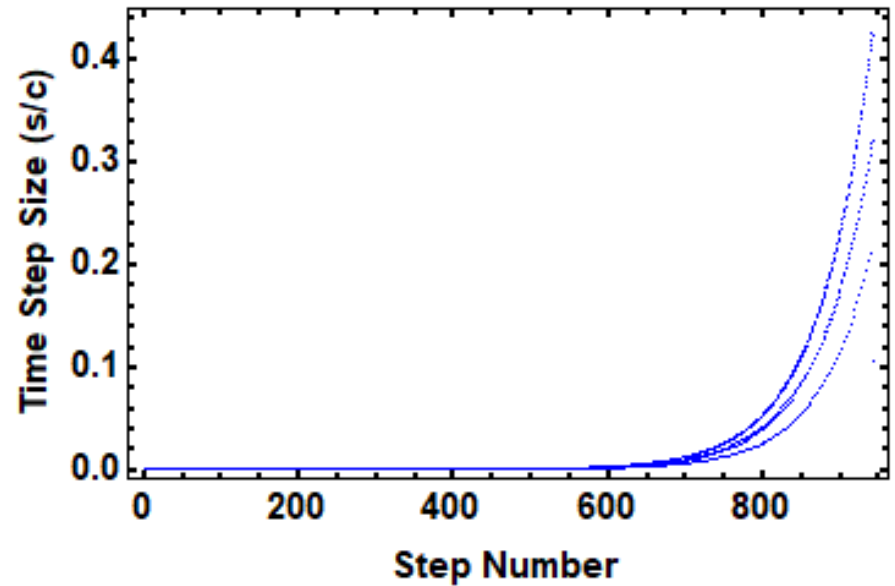
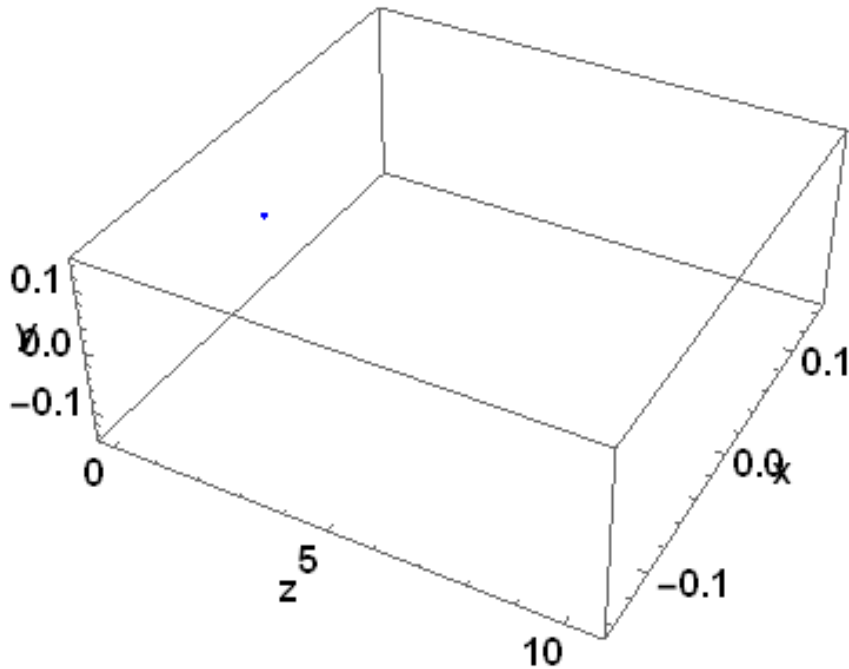
- Particle # 500



High Energy Lead Ions

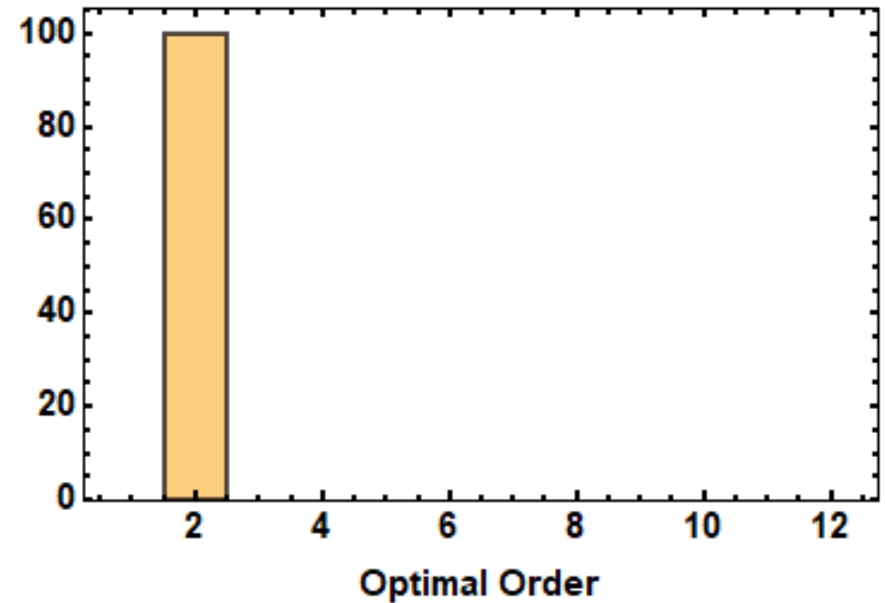
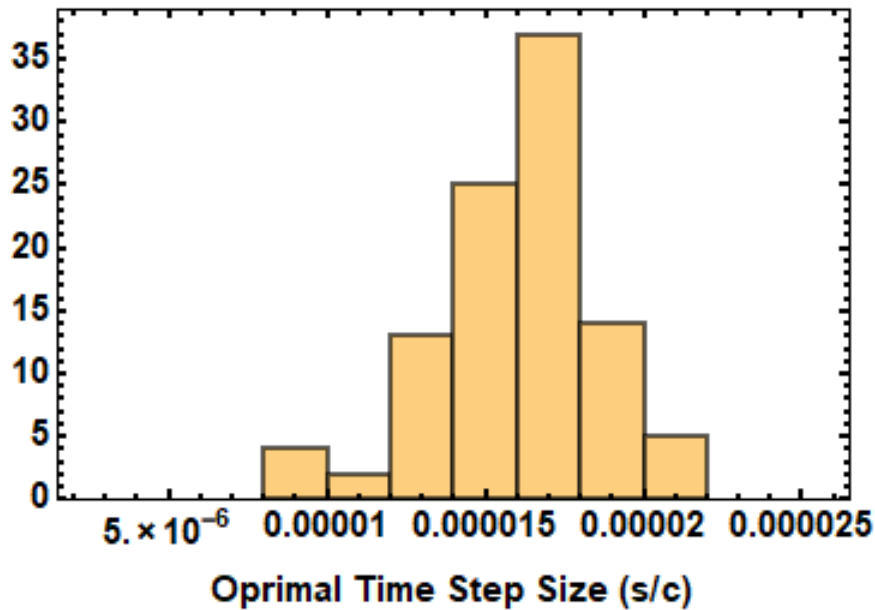


• Not Propagated • Propagated

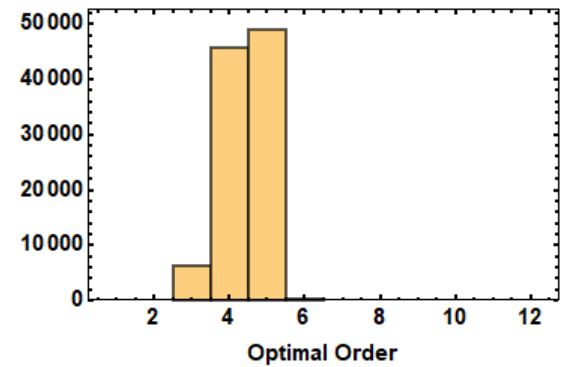
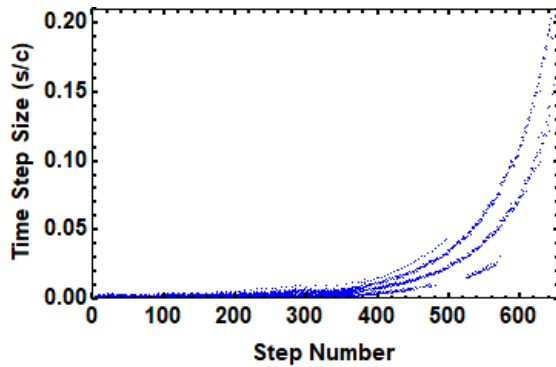
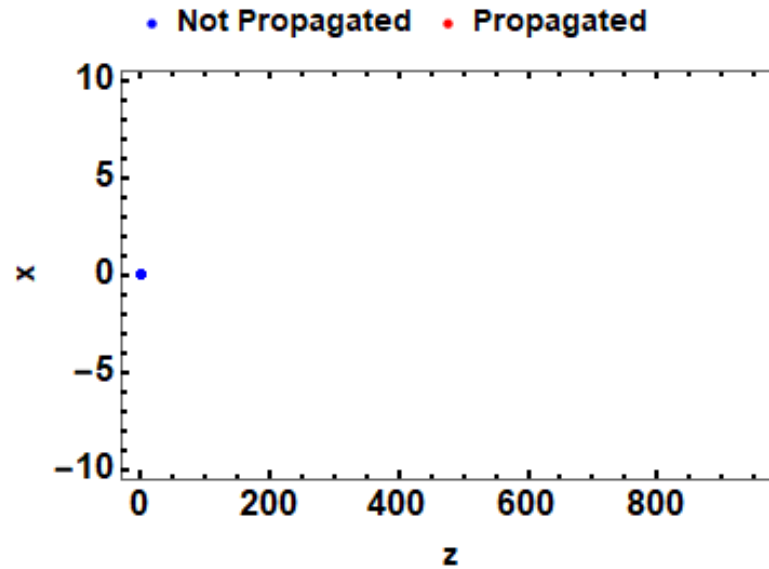


Accuracy setting $\varepsilon = 10^{-5}$

Optimal Time Step Sizes and Orders



Relativistic Electrons

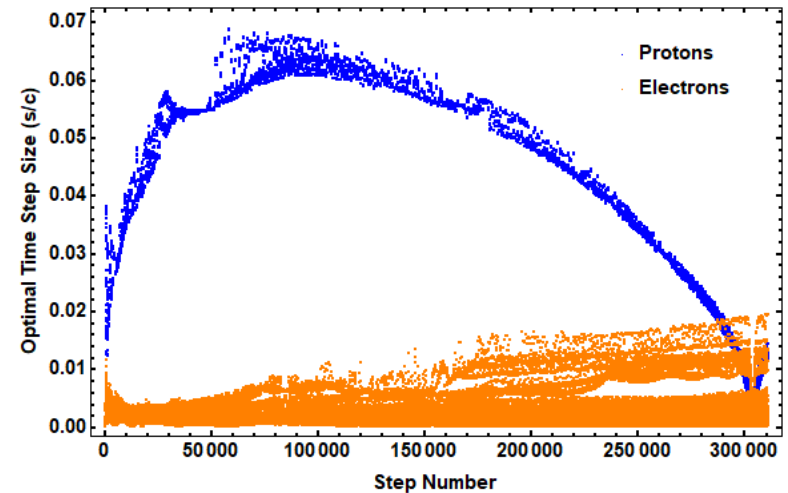
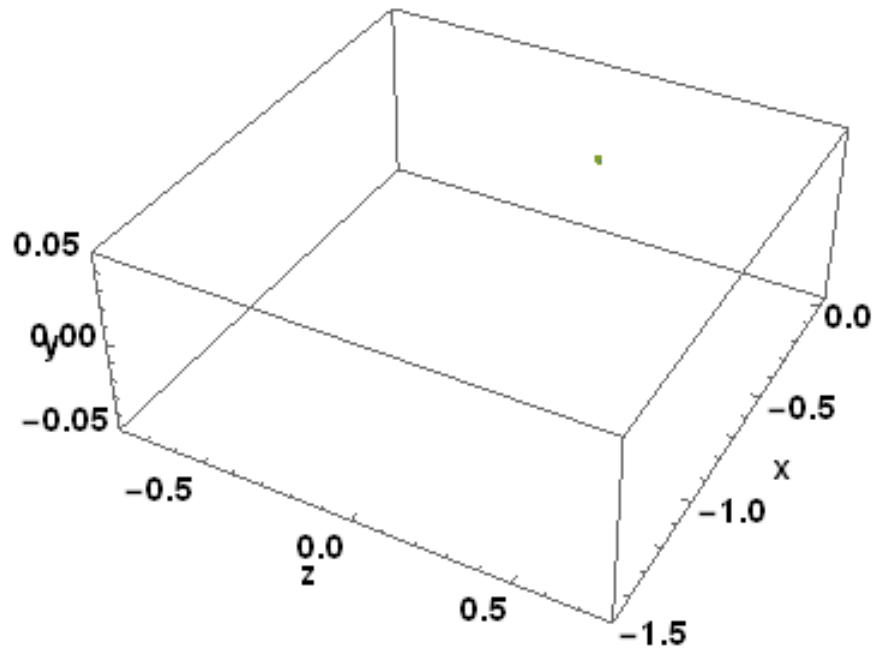


Accuracy setting $\varepsilon = 10^{-16}$

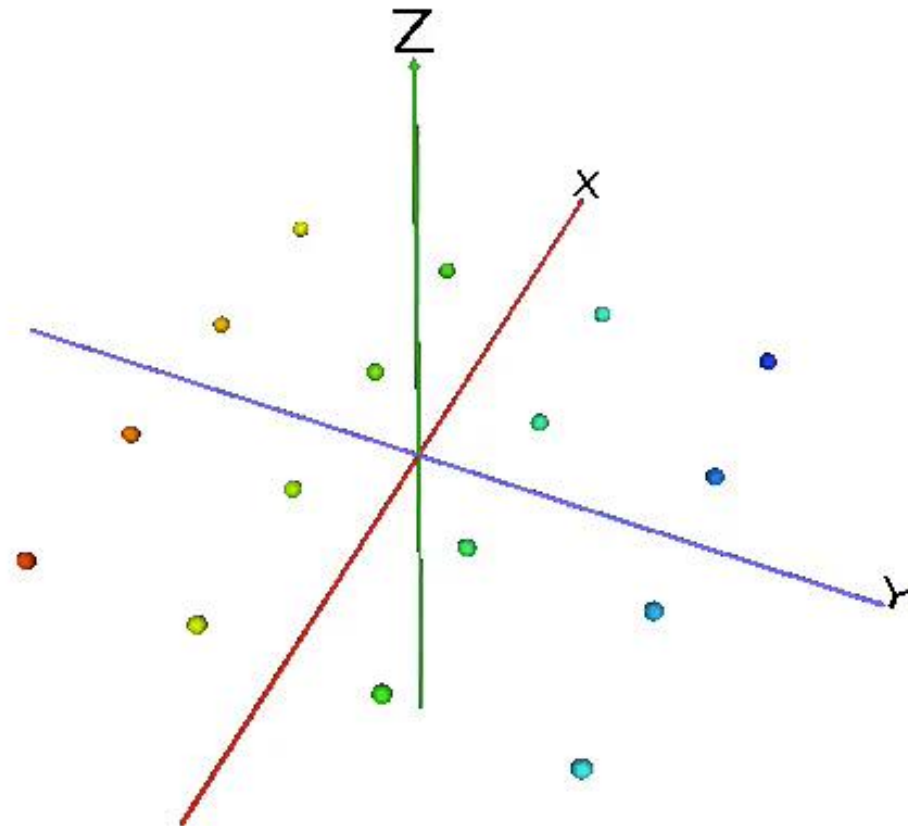
Protons and electrons in magnetic field



- Not-Propagated Protons • Propagated Protons
- Not-Propagated Electrons • Propagated Electrons



Head-On Collisions



Summary and Conclusions



- **Computational beam physics** plays an important part in modeling and simulating electron cooling; designing, operating, and improving current and future particle accelerators and their performance
- **Algorithmic and hardware improvements multiply**, making high fidelity large-scale problems feasible
- **Fundamental algorithms** and methods are general enough to be adaptable/applicable to many other beam dynamics problems and different scientific fields:
 - Current and next generation **high-performance computing** systems are well matched to these algorithms
 - Entering a new phase of **high fidelity *electron cooling simulations***